

**Nonlinear Optical Physics**  
*especially*  
**“Slow” and “Fast” Light in**  
**Room-Temperature Solids**

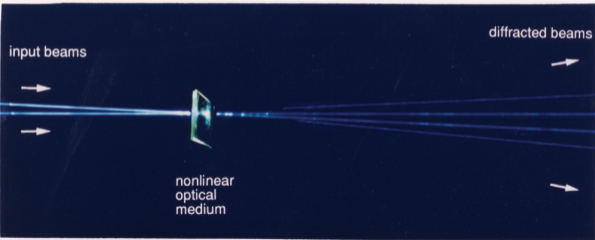
**Robert W. Boyd**

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<http://www.optics.rochester.edu>

Presented at the DAMOP, Boulder Colorado, May 22, 2003

# The Essence of Nonlinear Optics

## Light-By-Light Scattering



# Interest in Slow Light

Fundamentals of optical physics

Intrigue: Can (group) refractive index really be  $10^6$ ?

Optical delay lines, optical storage, optical memories

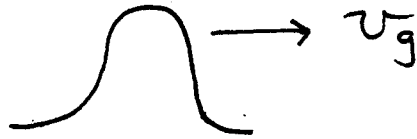
Implications for quantum information

# Slow Light

**group velocity  $\neq$  phase velocity**

# Group Velocity

Pulse  
(wave packet)



Group velocity given by  $v_g = \frac{d\omega}{dk}$

$$\text{For } k = \frac{n\omega}{c} \quad \frac{dk}{d\omega} = \frac{1}{c} \left( n + \omega \frac{dn}{d\omega} \right)$$

Thus

$$v_g = \frac{c}{n + \omega \frac{dn}{d\omega}} \equiv \frac{c}{n_g}$$

Thus  $n_g \neq n$  in a dispersive medium!

# Light Propagation in Atomic Vapors

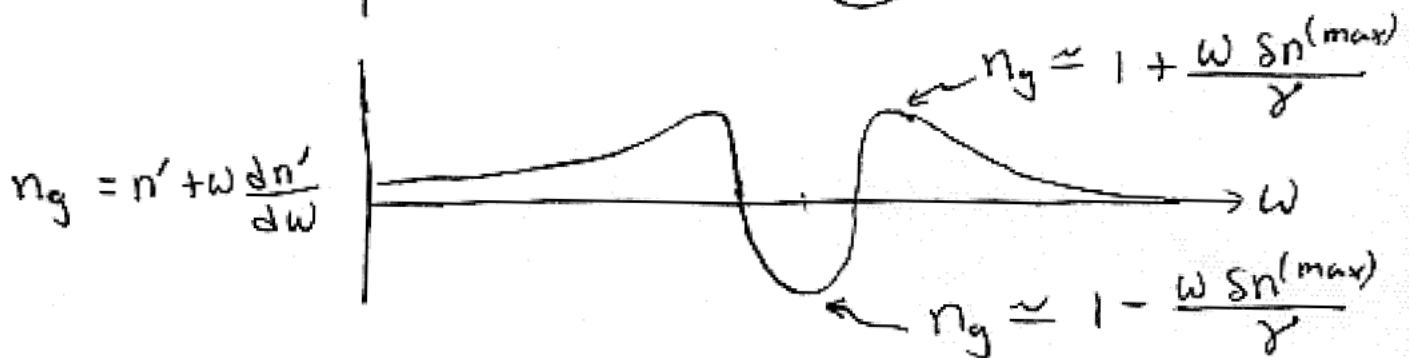
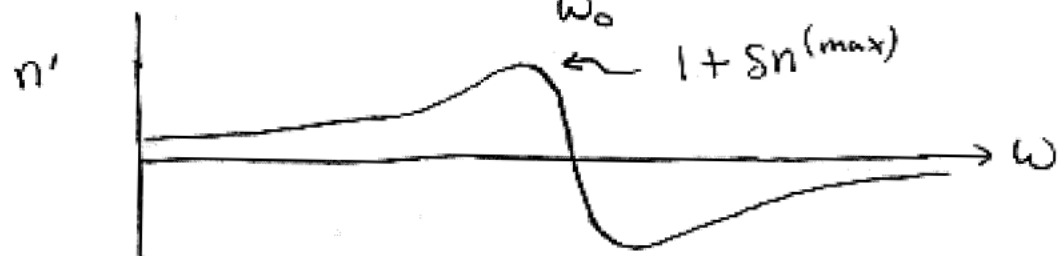
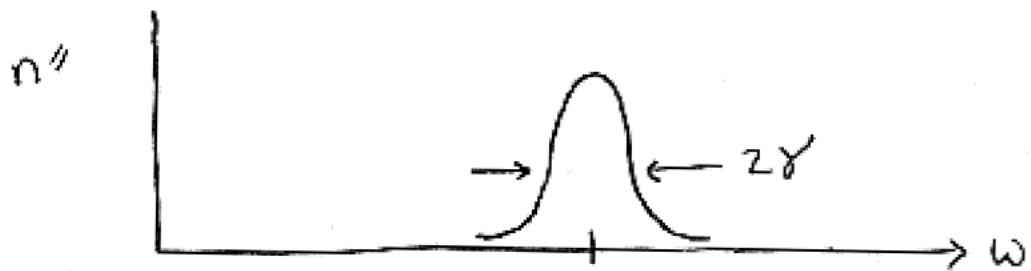
$$n = \sqrt{\epsilon} = \sqrt{1 + 4\pi\chi}$$

$$\chi = \frac{Ne^2 / 2m\omega_0}{(\omega_0 - \omega) - i\gamma}$$

For  $N$  not too large,  $n = n' + in'' \approx 1 + 2\pi\chi$

$$n' \approx 1 + \frac{\pi Ne^2}{m\omega_0} \frac{\omega_0 - \omega}{(\omega_0 - \omega)^2 + \gamma^2}$$

$$n'' = \frac{\pi Ne^2}{2m\omega_0\gamma} \frac{\gamma^2}{(\omega_0 - \omega)^2 + \gamma^2}$$



$$\frac{\omega \delta n^{(max)}}{\gamma} \approx \frac{2\pi(5 \times 10^{14})(0.1)}{2\pi(1 \times 10^9)} = 5 \times 10^4 \sim (!)$$

$n_g$  can range from  $+5 \times 10^4$  to  $-5 \times 10^4$ .

(But with lots of absorption)

## How to Produce Slow Light?

Group index can be as large as

$$n_g \approx 1 + \frac{\omega \text{sn}^{(\max)}}{\gamma}$$

Use Nonlinear optics to

(1) decrease line width  $\gamma$   
(produce sub-Doppler linewidth)

(2) decrease absorption  
(so transmitted pulse is detectable)

# Slow Light in Atomic Media

Slow light propagation in atomic media (vapors and BEC), facilitated by quantum coherence effects, has been successfully observed by many groups.



# Challenge/Goal

Slow light in room-temperature solid-state material.

- Slow light in room temperature ruby  
(facilitated by a novel quantum coherence effect)
- Slow light in a structured waveguide

# Slow Light in Ruby

Need a large  $dn/d\omega$ . (How?)

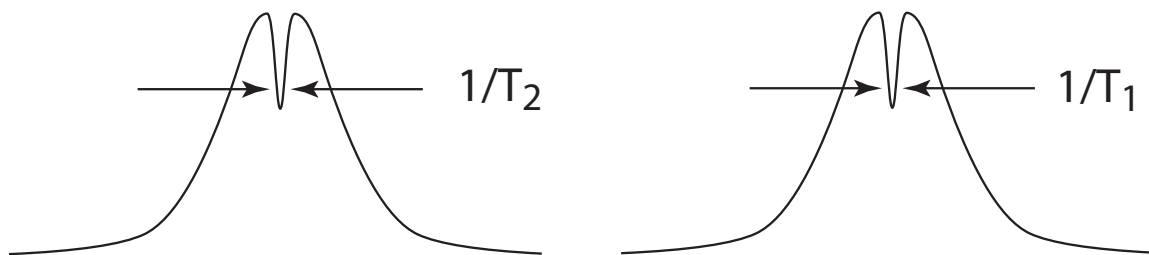
Kramers-Kronig relations:

Want a very narrow absorption line.

Well-known (to the few people how know it well) how to do so:

Make use of “spectral holes” due to population oscillations.

Hole-burning in a homogeneously broadened line; requires  $T_2 \ll T_1$ .

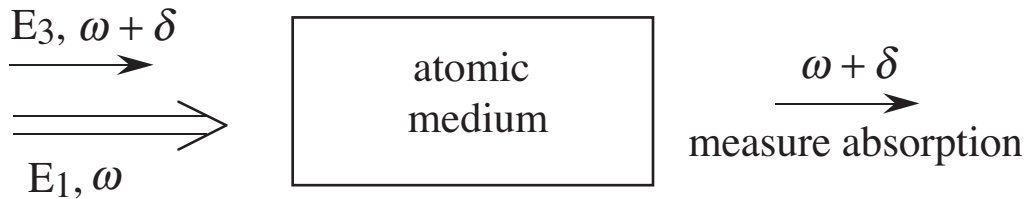
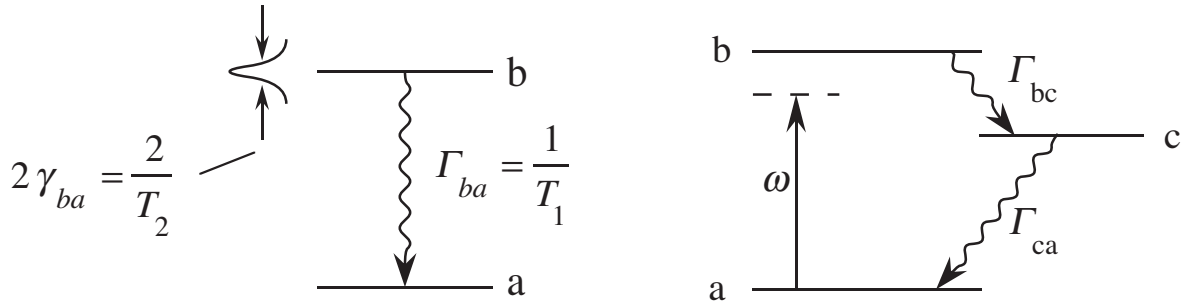


inhomogeneously  
broadened medium

homogeneously  
broadened medium  
(or inhomogeneously  
broadened)

PRL 90,113903(2003); see also news story in Nature.

# Spectral Holes Due to Population Oscillations



Population inversion:

$$(\rho_{bb} - \rho_{aa}) = w \quad w(t) \approx w^{(0)} + w^{(-\delta)} e^{i\delta t} + w^{(\delta)} e^{-i\delta t}$$

population oscillation terms important only for  $\delta \leq 1/T_1$

Probe-beam response:

$$\rho_{ba}(\omega + \delta) = \frac{\mu_{ba}}{\hbar} \frac{1}{\omega - \omega_{ba} + i/T_2} \left[ E_3 w^{(0)} + E_1 w^{(\delta)} \right]$$

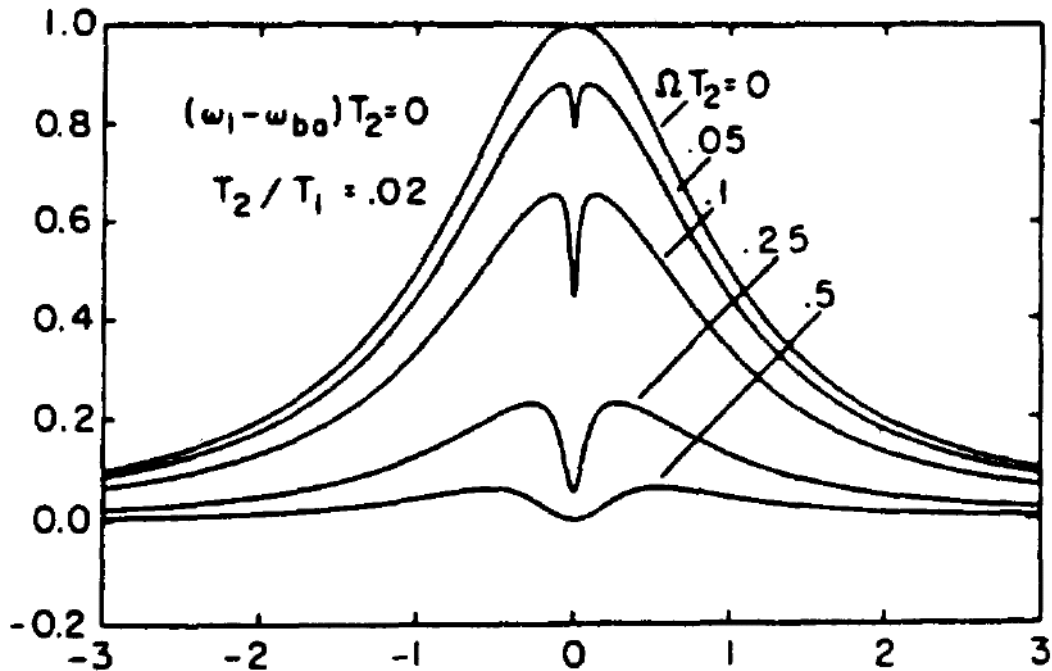
Probe-beam absorption:

$$\alpha(\omega + \delta) \propto \left[ w^{(0)} - \frac{\Omega^2 T_2}{T_1} \frac{1}{\delta^2 + \beta^2} \right]$$

linewidth  $\beta = (1/T_1)(1 + \Omega^2 T_1 T_2)$

# Spectral Holes in Homogeneously Broadened Materials

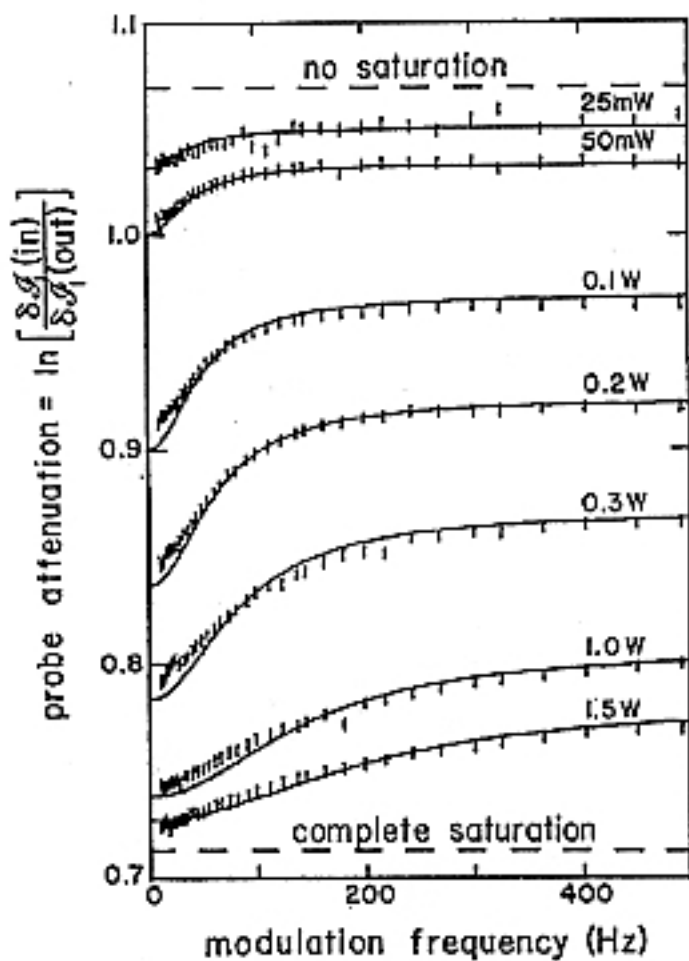
Occurs only in collisionally broadened media ( $T_2 \ll T_1$ )



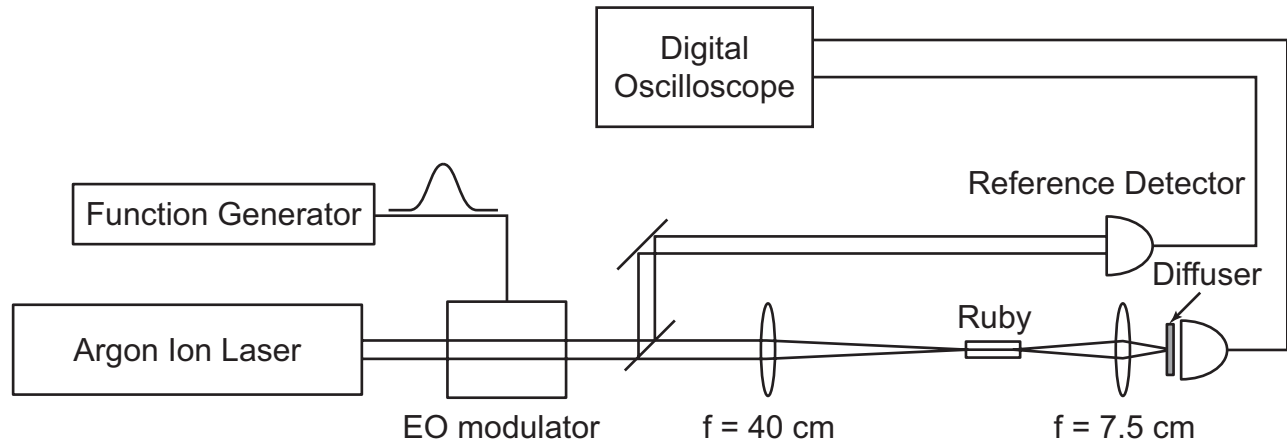
Boyd, Raymer, Narum and Harter, Phys. Rev. A24, 411, 1981.

**OBSERVATION OF A SPECTRAL HOLE DUE TO POPULATION OSCILLATIONS  
IN A HOMOGENEOUSLY BROADENED OPTICAL ABSORPTION LINE**

Lloyd W. HILLMAN, Robert W. BOYD, Jerzy KRASINSKI and C.R. STROUD, Jr.  
*The Institute of Optics, University of Rochester, Rochester, NY 14627, USA*

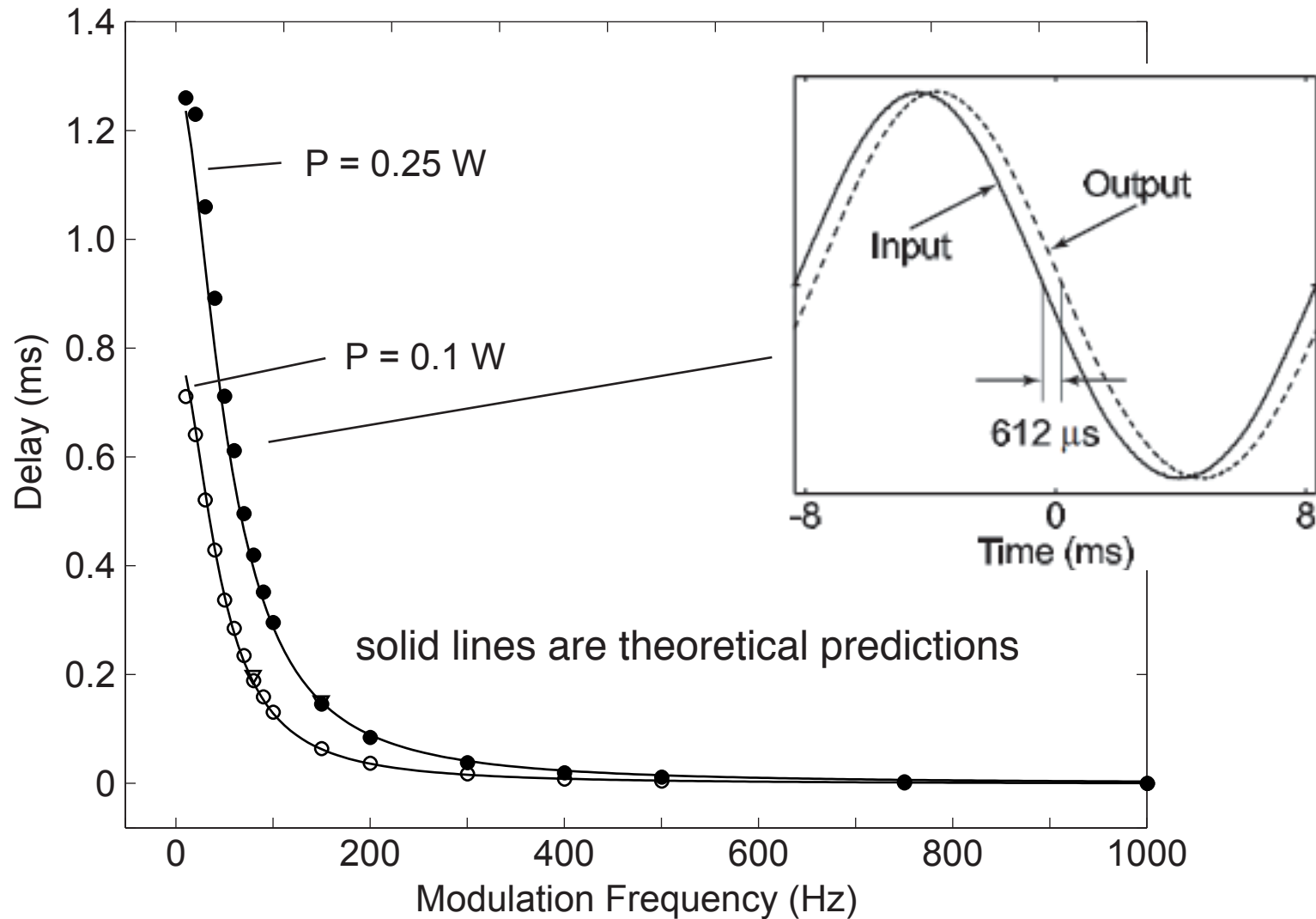


# Experimental Setup Used to Observe Slow Light in Ruby



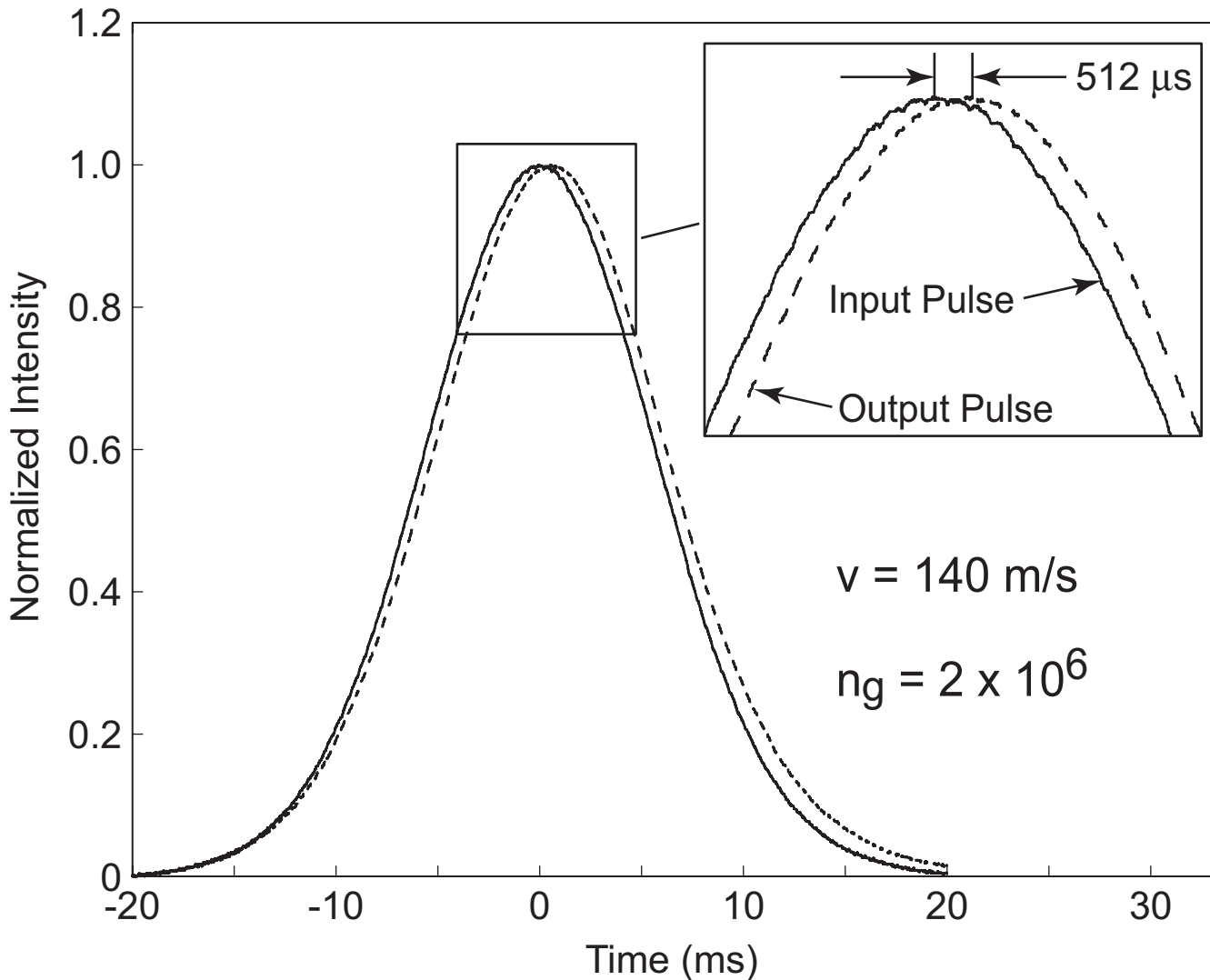
7.25 cm ruby laser rod (pink ruby)

# Measurement of Delay Time for Harmonic Modulation



For 1.2 ms delay,  $v = 60 \text{ m/s}$  and  $n_g = 5 \times 10^6$

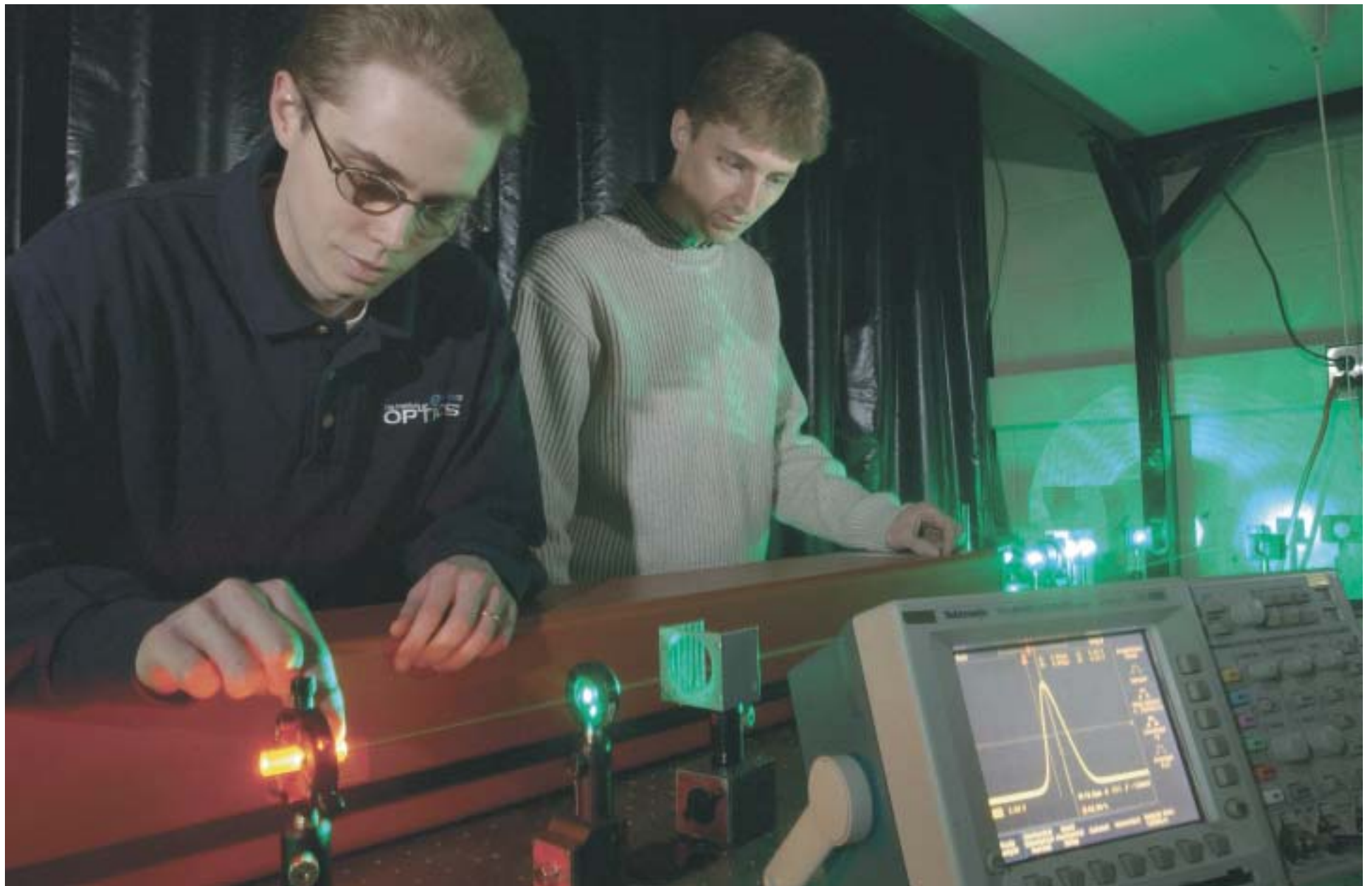
# Gaussian Pulse Propagation Through Ruby



No pulse distortion!

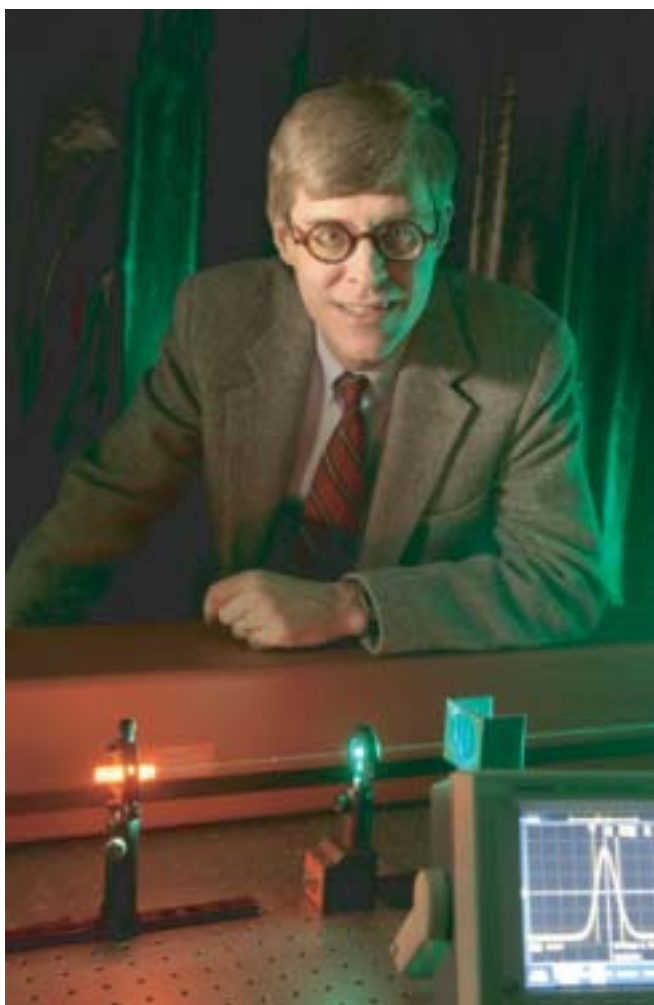


# Matt Bigelow and Nick Lepeshkin in the Lab



# Comparison of University of Rochester and University of Arizona

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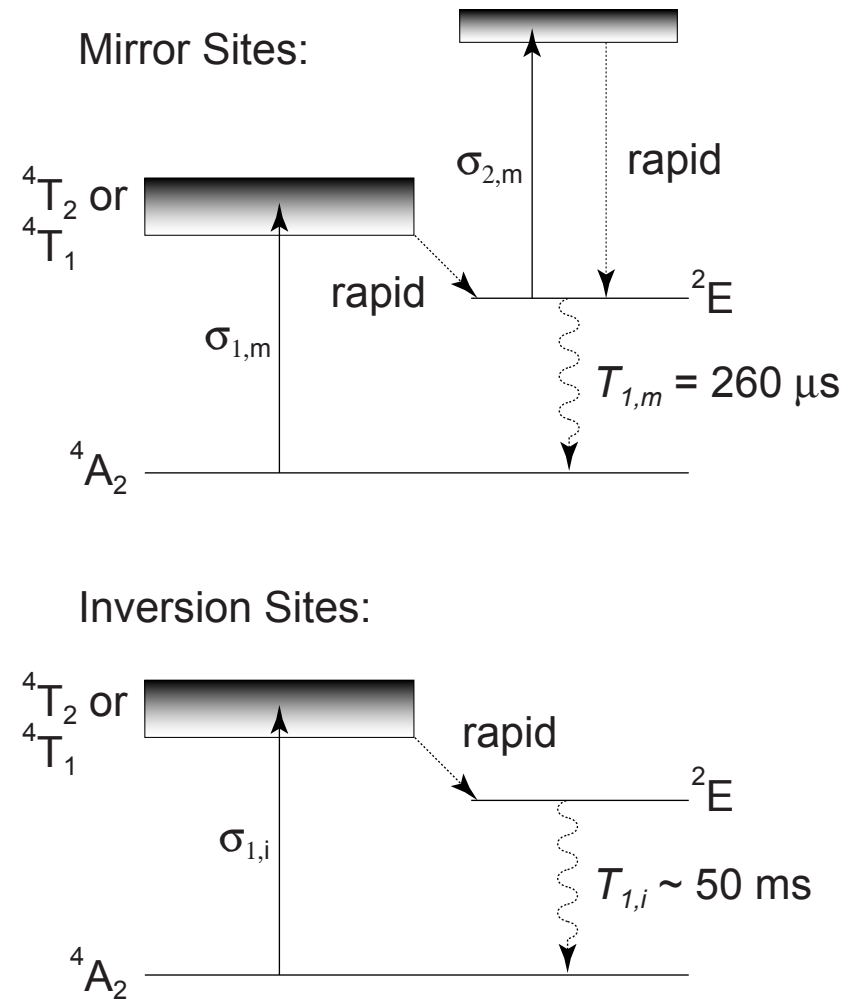
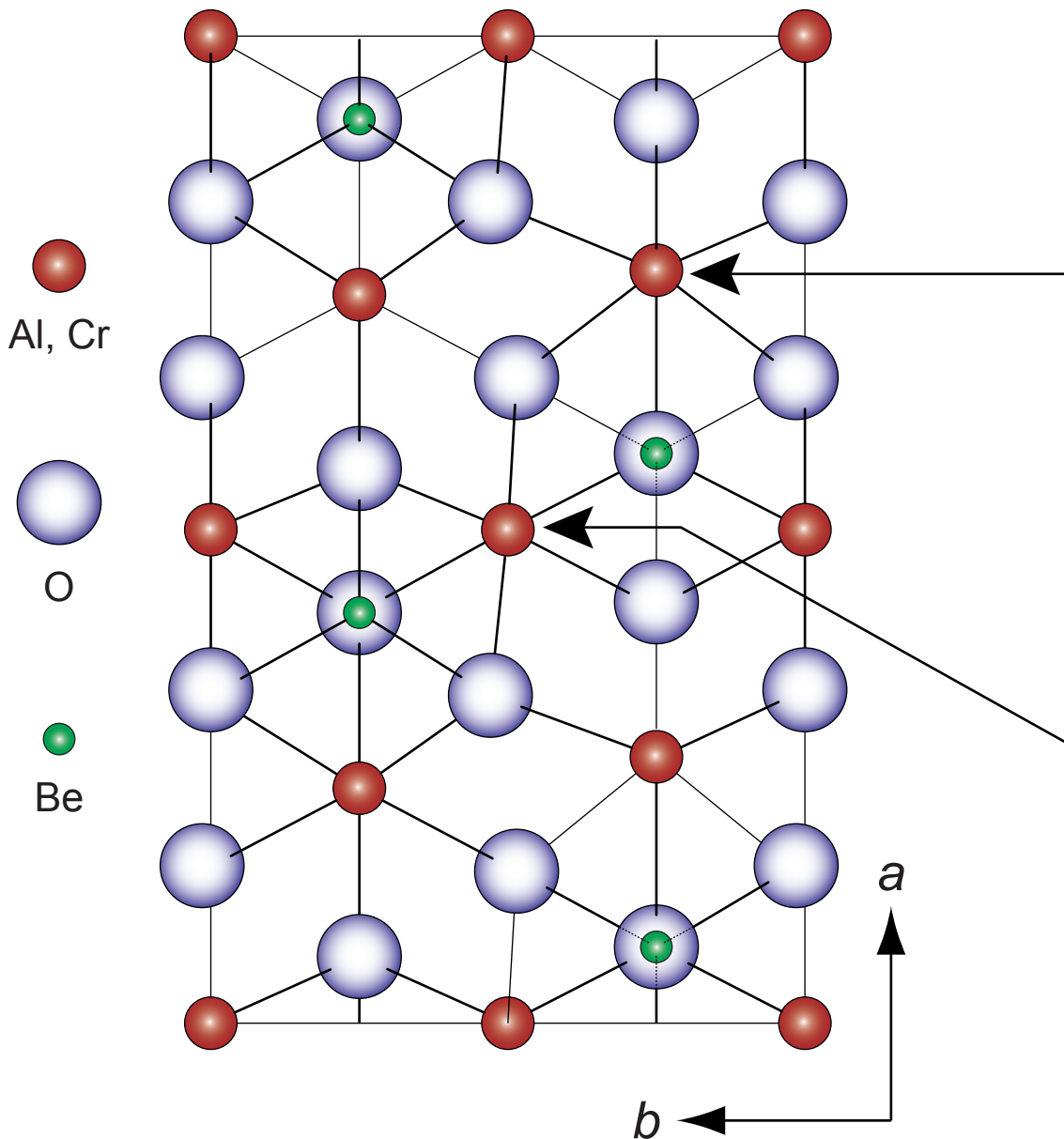


Bob and Ruby



Hyatt and Galina

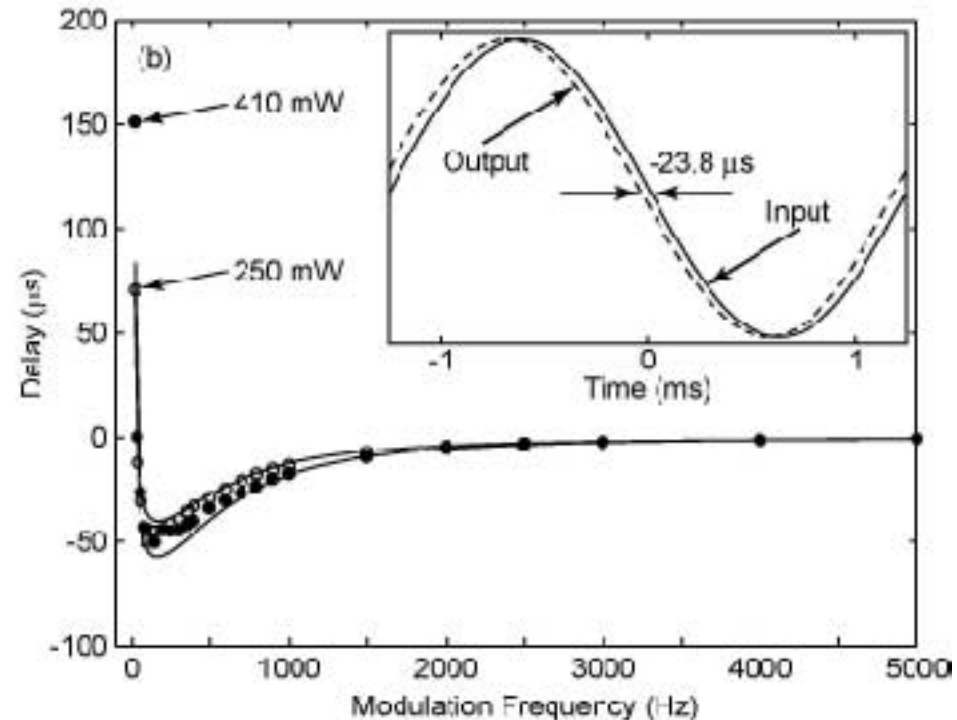
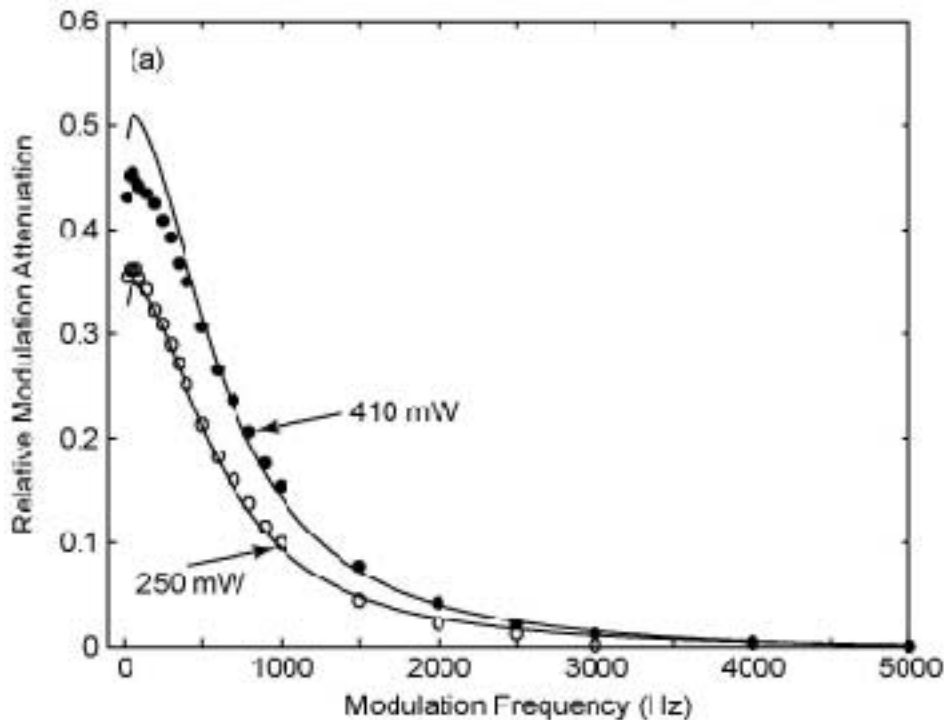
# Alexandrite Displays both Saturable and Inverse-Saturable Absorption



# Inverse-Saturable Absorption Produces Superluminal Propagation in Alexandrite

At 476 nm, alexandrite is an inverse saturable absorber

Negative time delay of 50  $\mu\text{s}$  corresponds to a velocity of -800 m/s



M. Bigelow, N. Lepeshkin, and RWB, accepted for publication, 2003

# Slow and Fast Light --What Next?

Longer fractional delay  
(saturate deeper; propagate farther)

Find material with faster response  
(technique works with shorter pulses)

# Artificial Materials for Nonlinear Optics

Artificial materials can produce  
Large nonlinear optical response  
Large dispersive effects

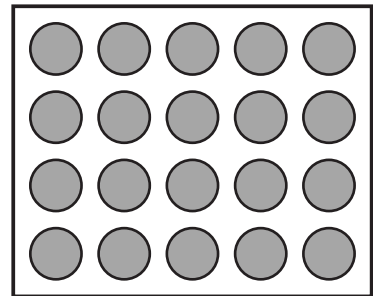
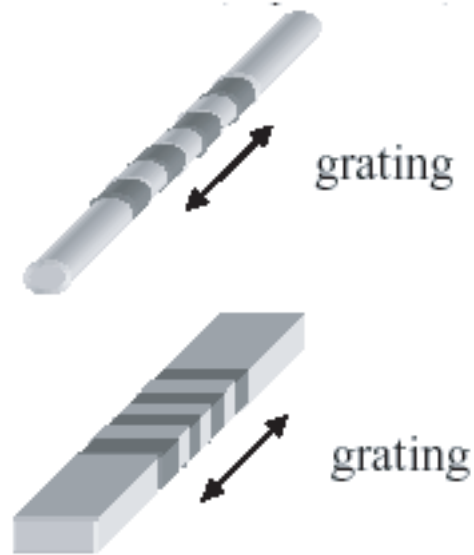
## Examples

Fiber/waveguide Bragg gratings

PBG materials

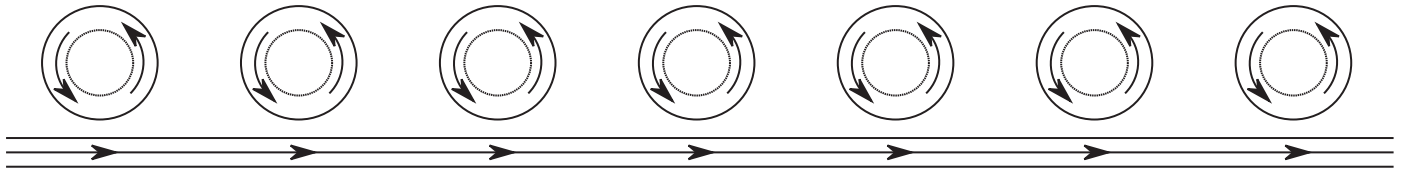
CROW devices (Yariv et al.)

SCISSOR devices



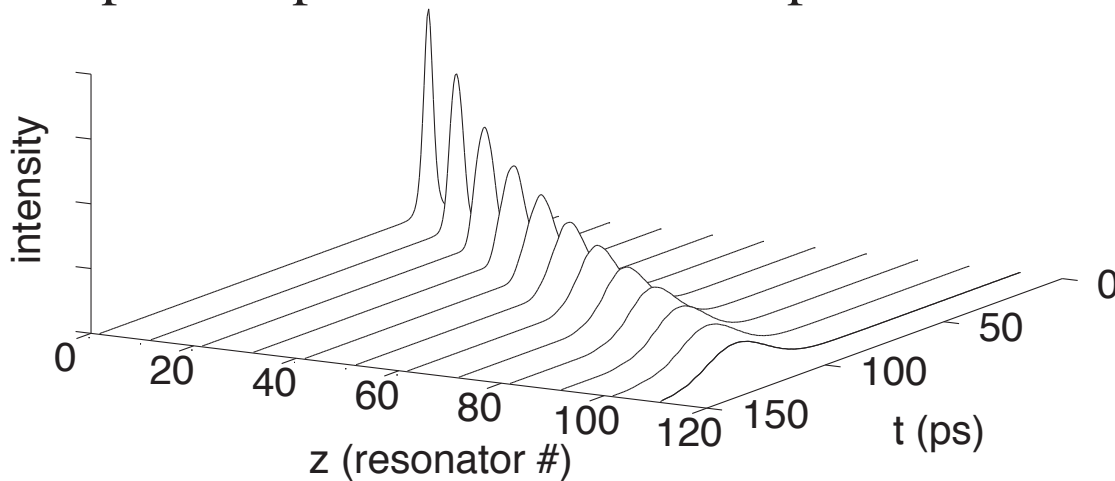
# NLO of SCISSOR Devices

(Side-Coupled Integrated Spaced Sequence of Resonators)

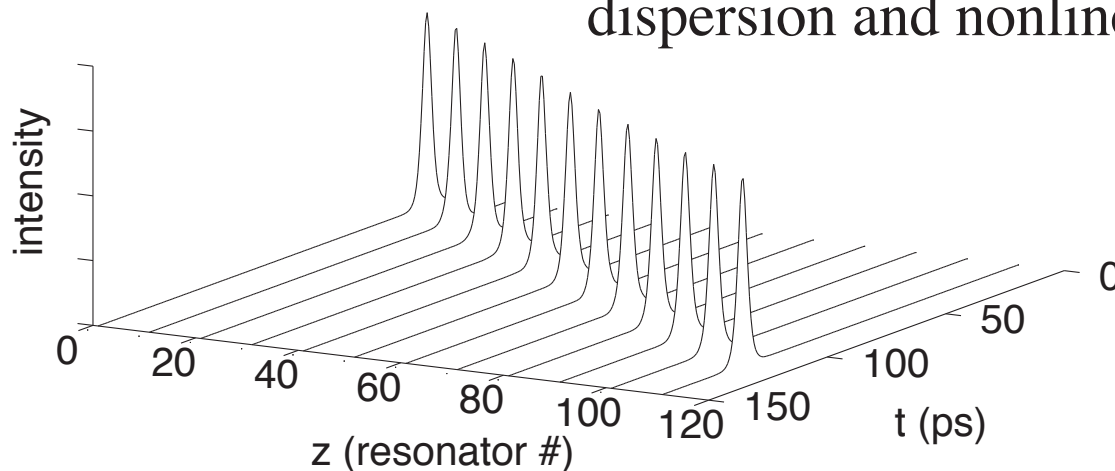


Shows slow-light, tailored dispersion, and enhanced nonlinearity  
Optical solitons described by nonlinear Schrodinger equation

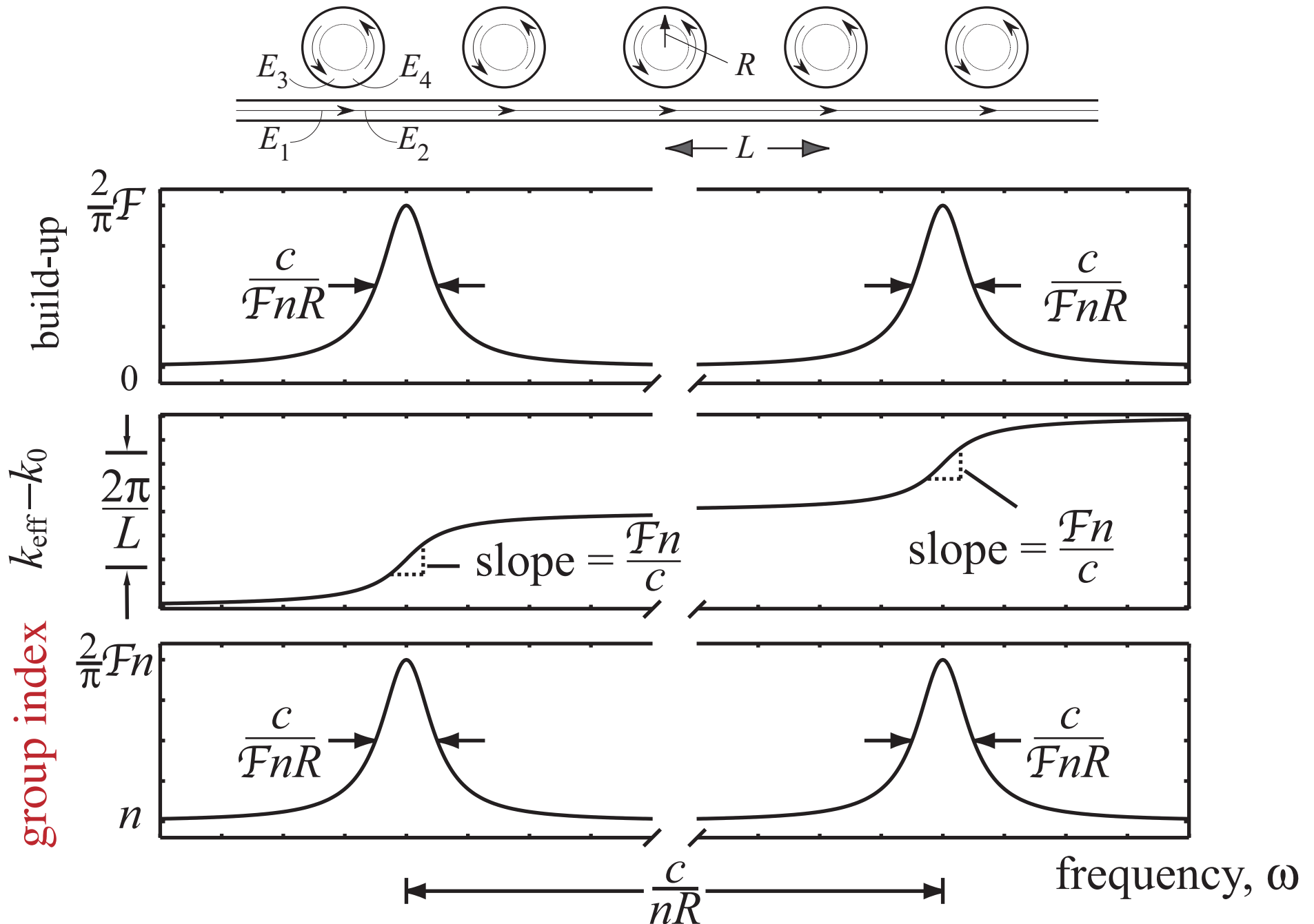
- Weak pulses spread because of dispersion



- But intense pulses form solitons through balance of dispersion and nonlinearity.



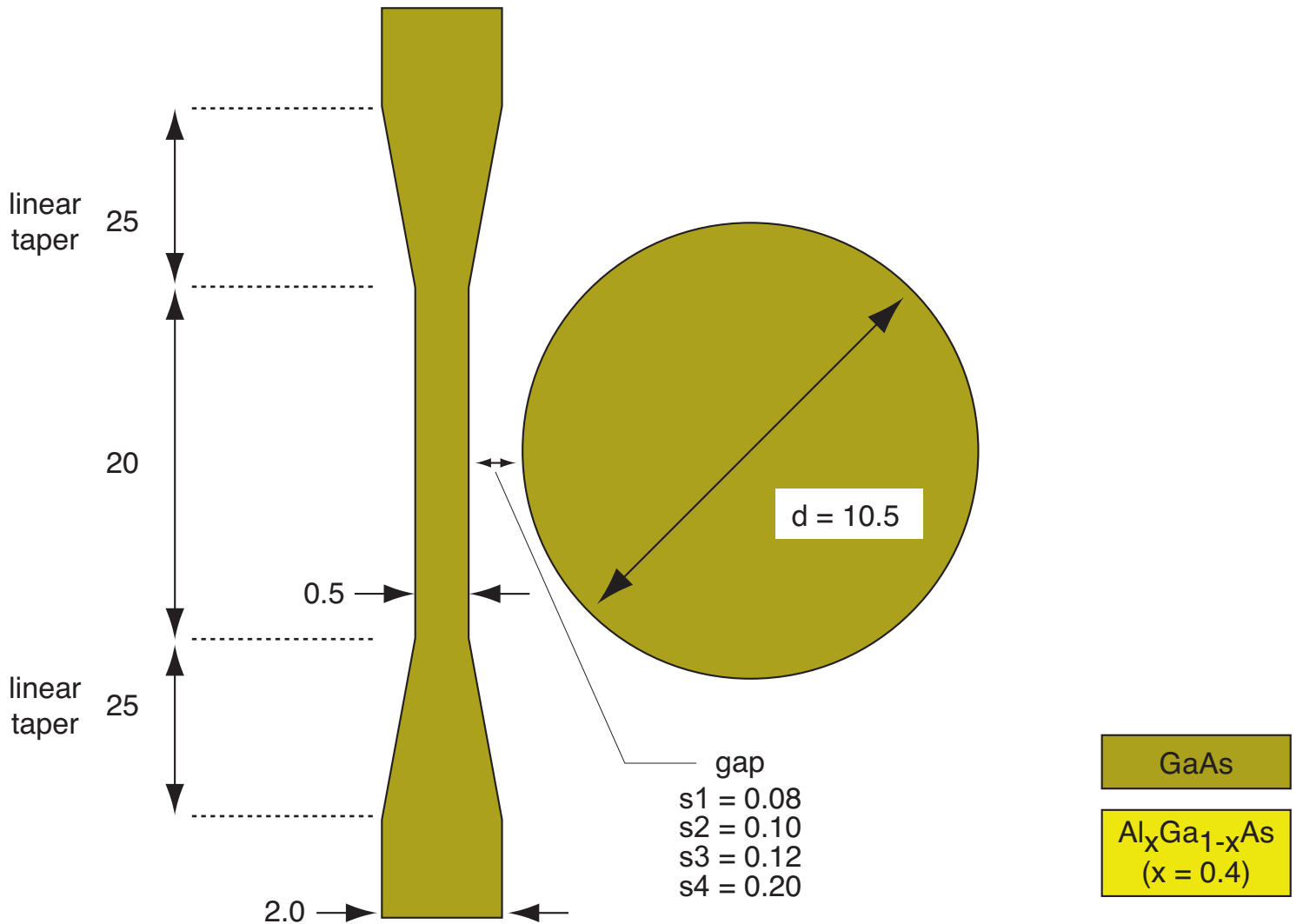
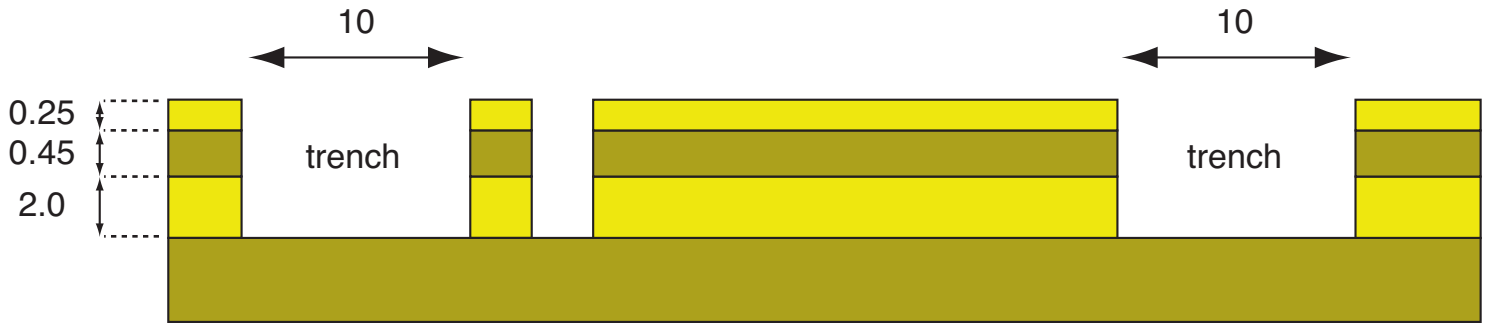
# Slow Light and SCISSOR Structures





# Microdisk Resonator Design

All dimensions in microns



# Photonic Device Fabrication Procedure

(1) MBE growth



(2) Deposit oxide



(3) Spin-coat e-beam resist



(4) Pattern inverse with e-beam & develop



(5) RIE etch oxide



(6) Remove PMMA



(7) CAIBE etch AlGaAs-GaAs

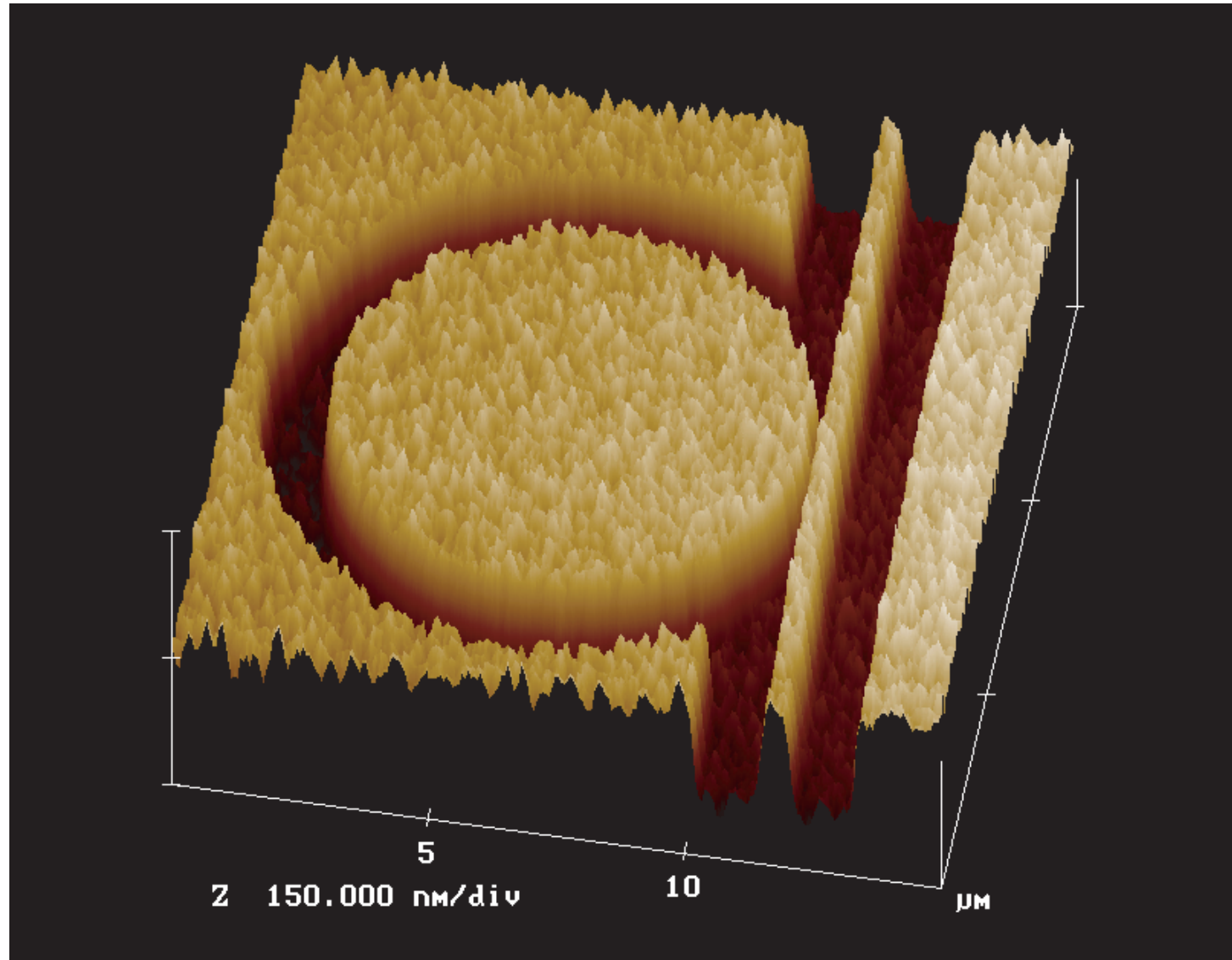


(8) Strip oxide



# Disk Resonator and Optical Waveguide in PMMA Resist

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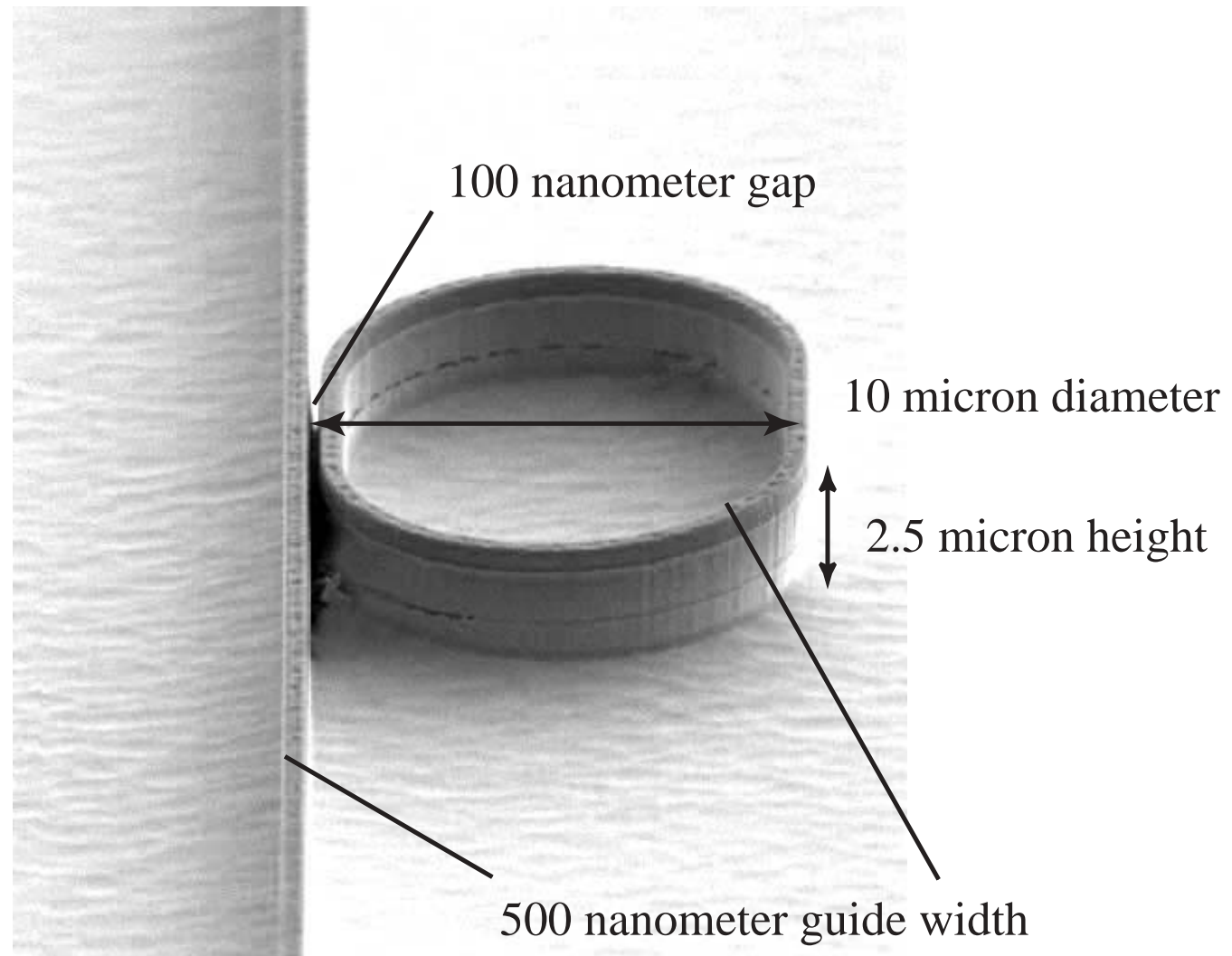


AFM

# All-Pass Racetrack Microresonator

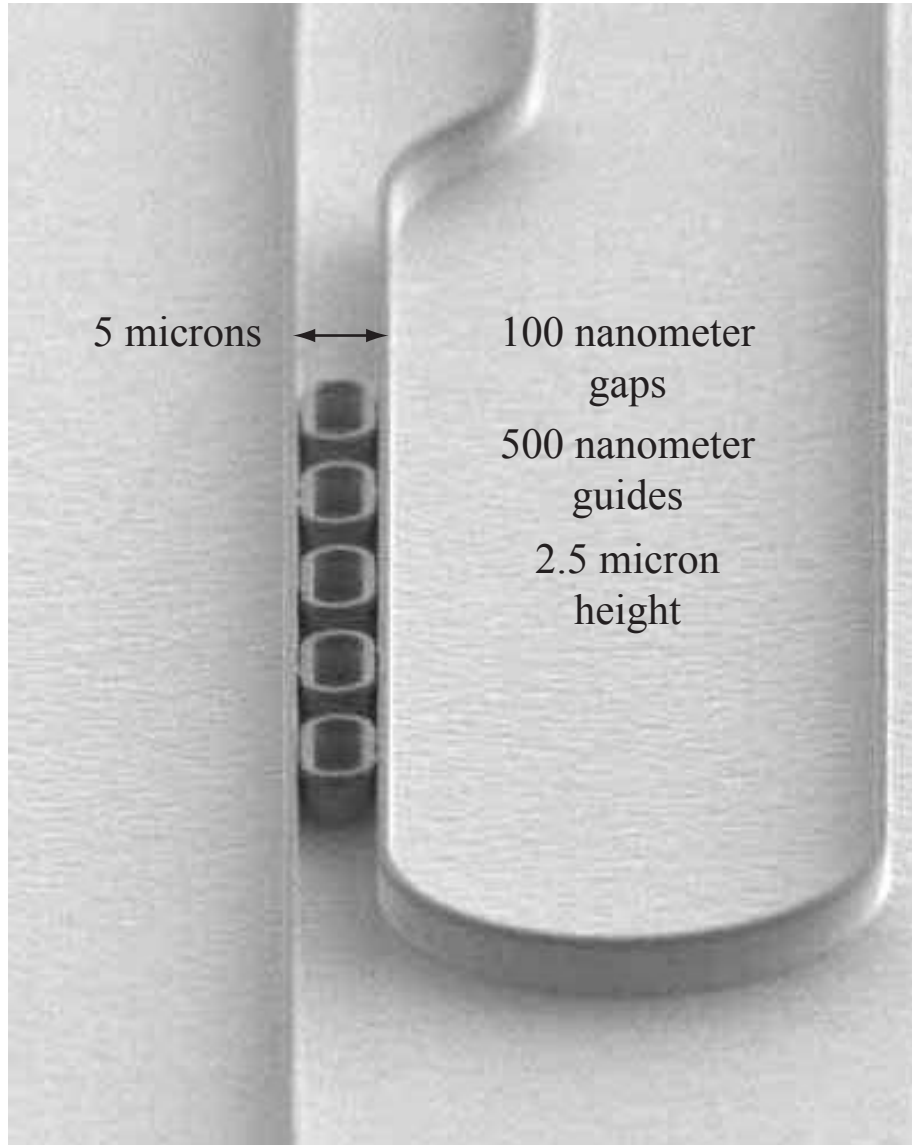
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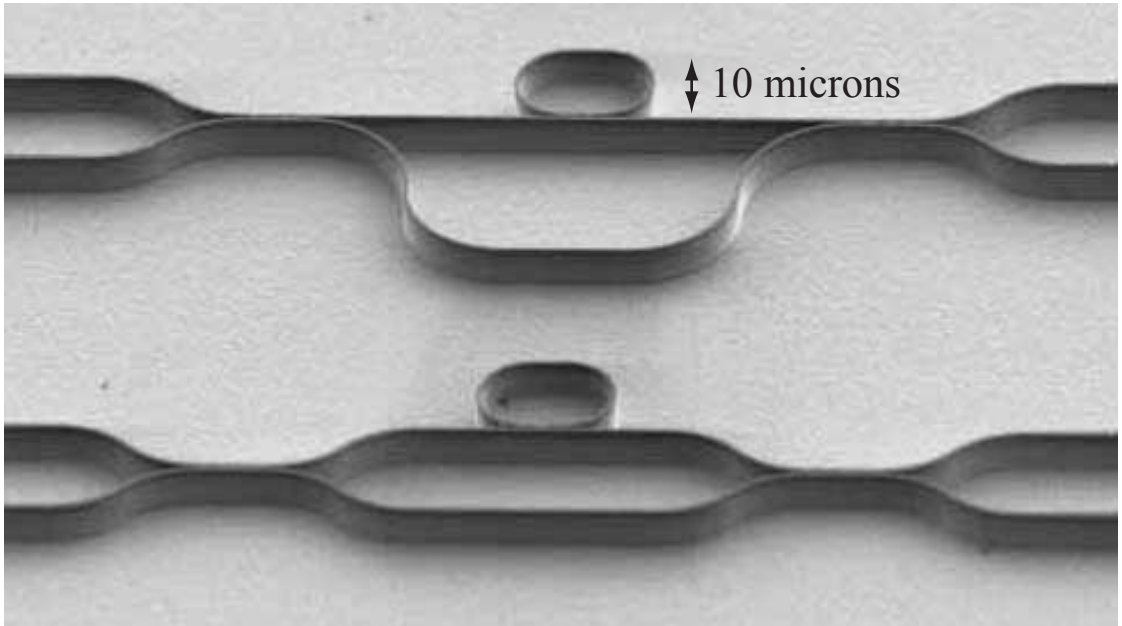


Thanks to P.T. Ho and R. Grover, U. Maryland, for help with final etch.

# Five-Cell SCISSOR with Tap Channel



# Resonator-Enhanced Mach-Zehnder Interferometers



~100 nanometer  
gaps

500 nanometer  
guides

2.5 micron  
height

# Laboratory Characterization of Photonic Structures

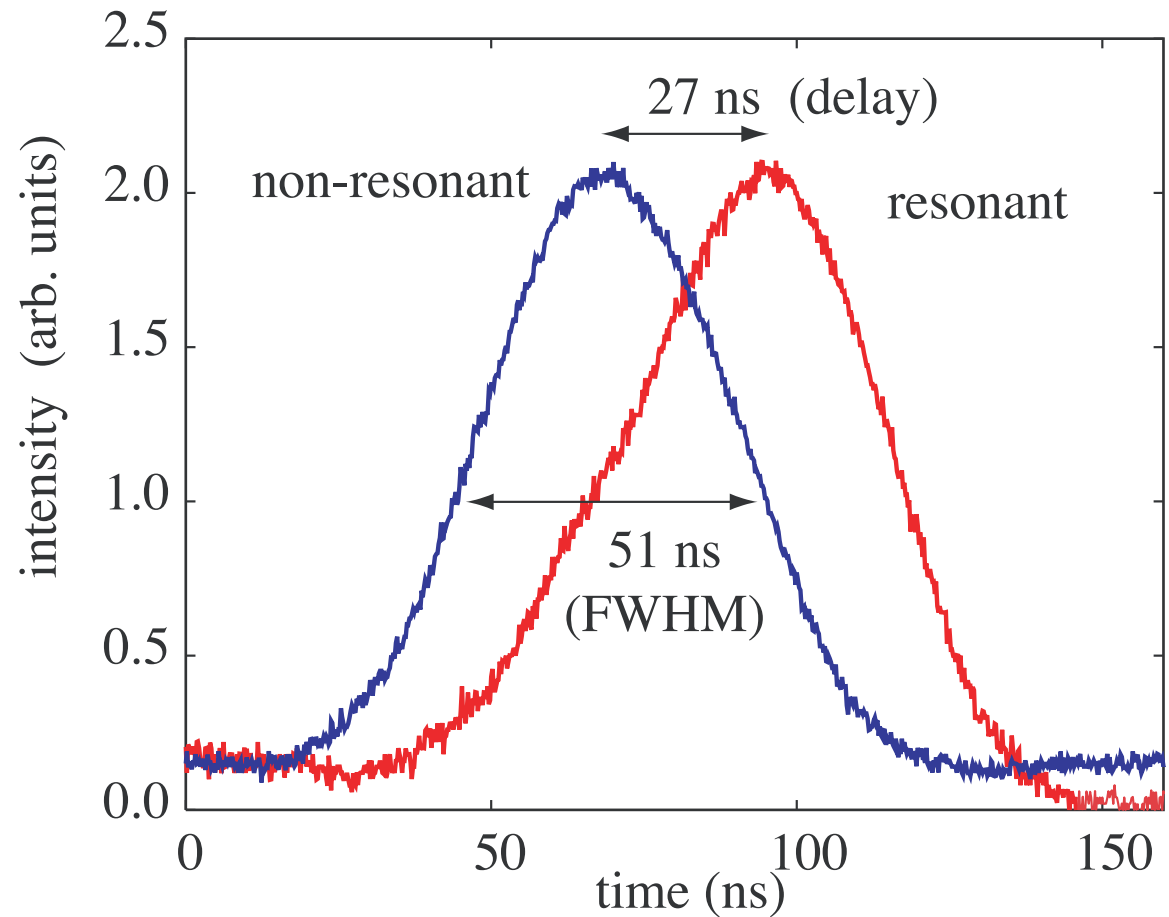
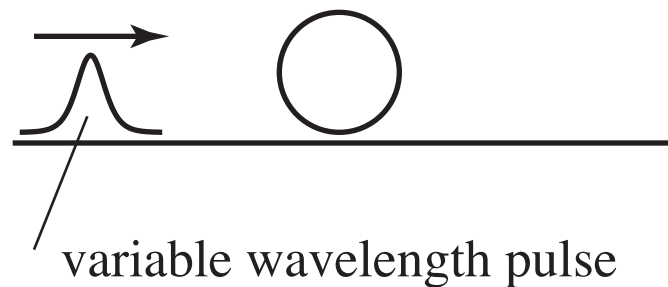
- Characterization of fiber ring-resonator devices  
(Proof of principle studies)
- Characterization of nanofabricated devices

# Fiber-Resonator Optical Delay Line

Fiber optical delay line:



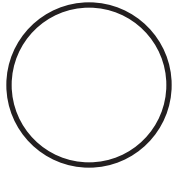
First study one element of optical delay line:





# Transmission Characteristics of Fiber Ring Resonator

circumference = 31 cm



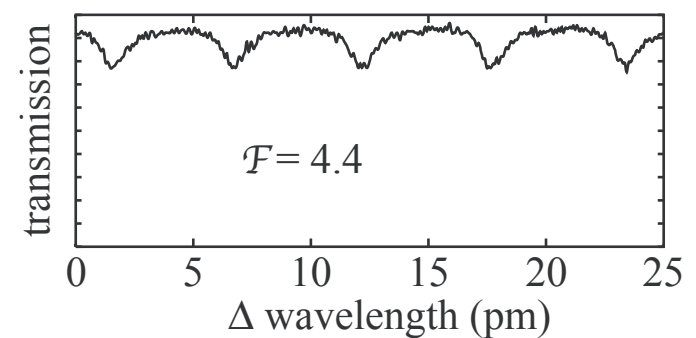
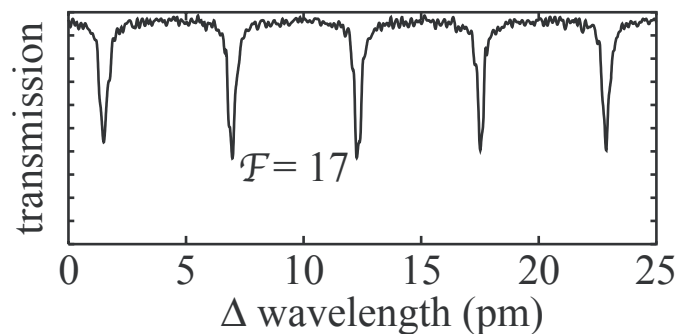
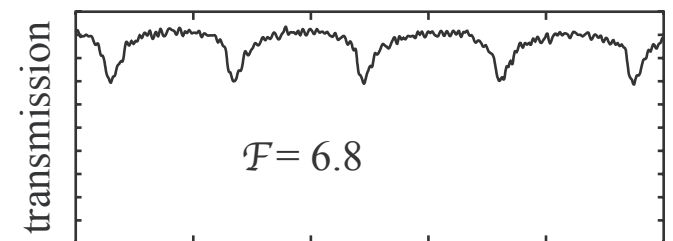
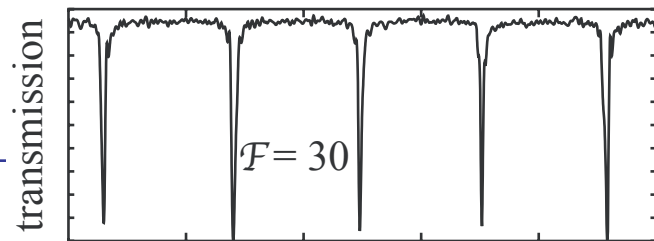
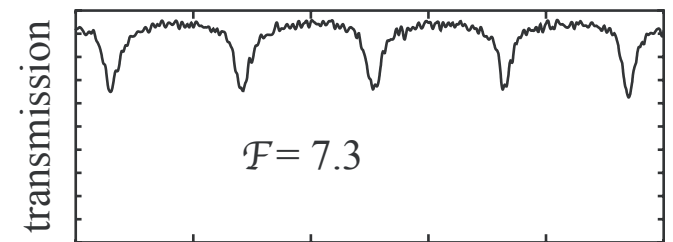
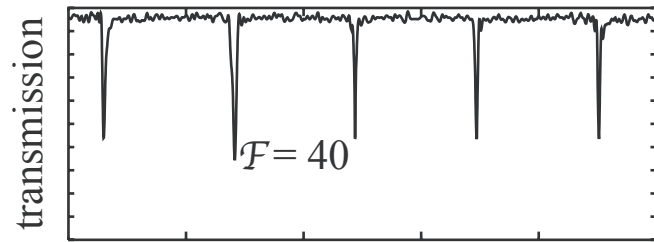
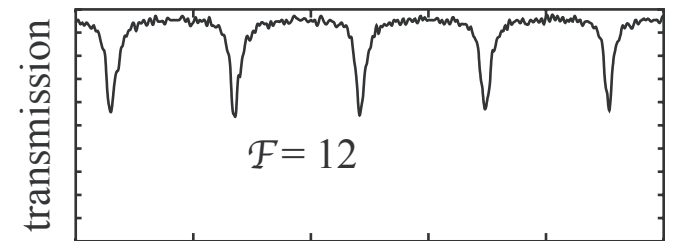
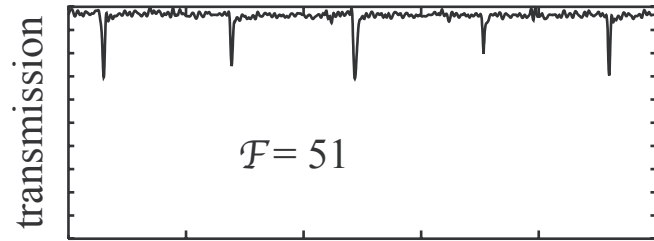
variable coupling

Measure transmission vs.  $\lambda$  for various values of the finesse

undercoupled

critically coupled

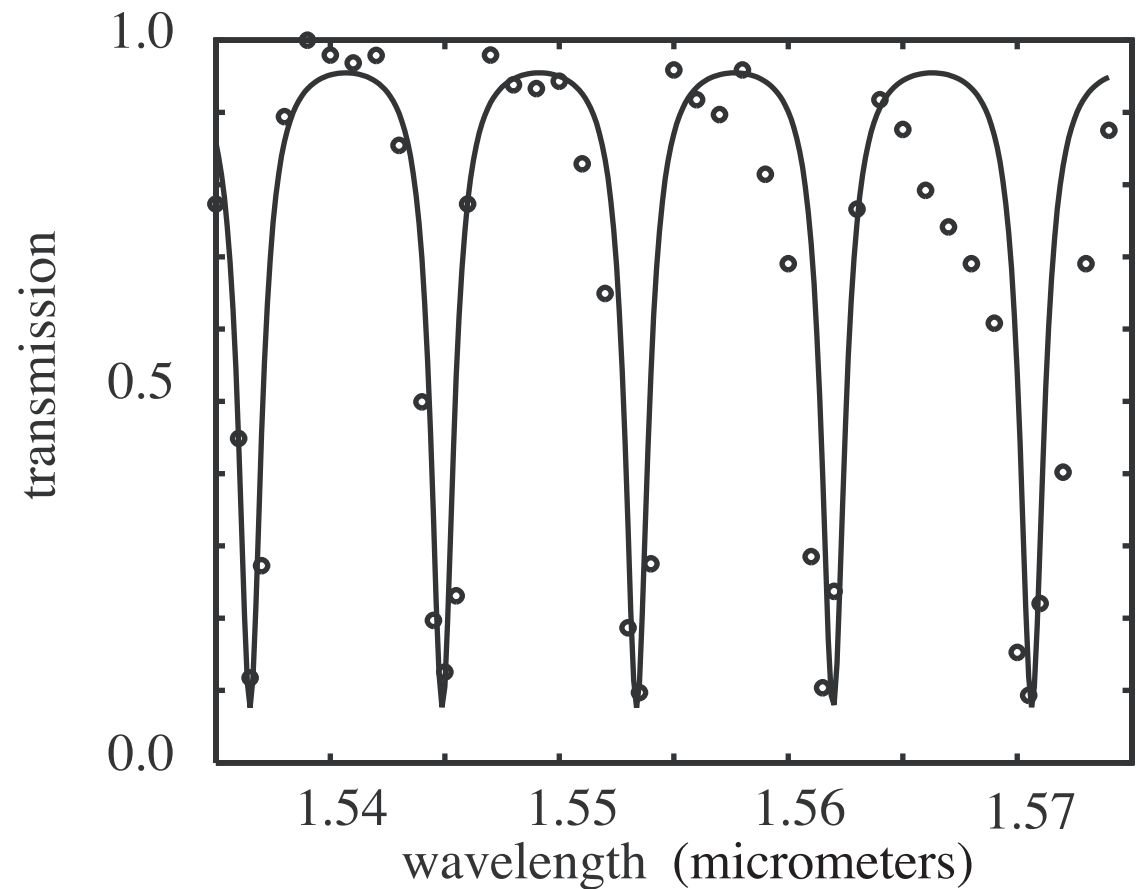
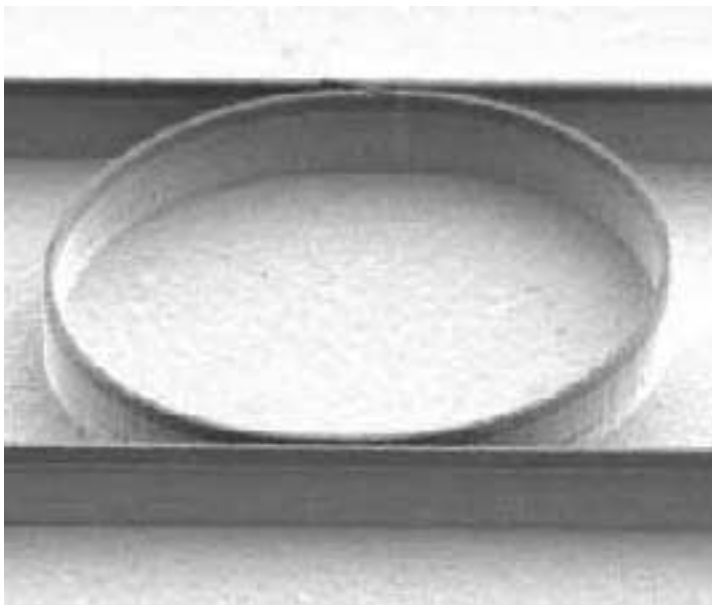
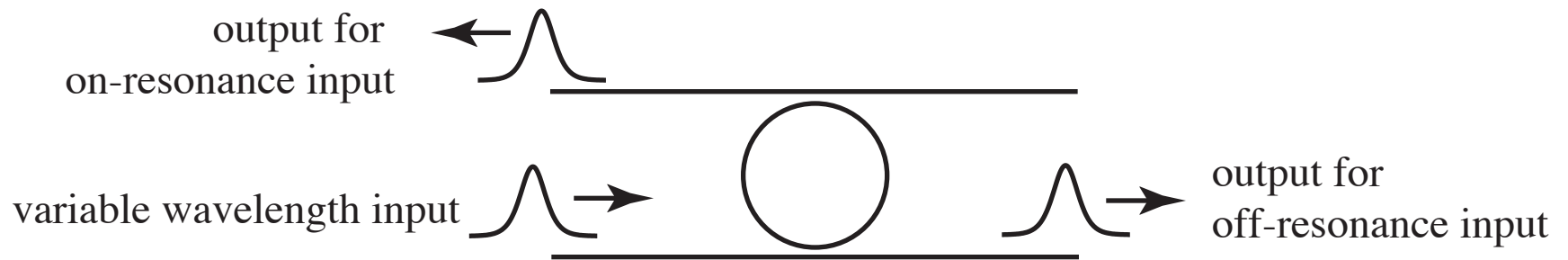
overcoupled



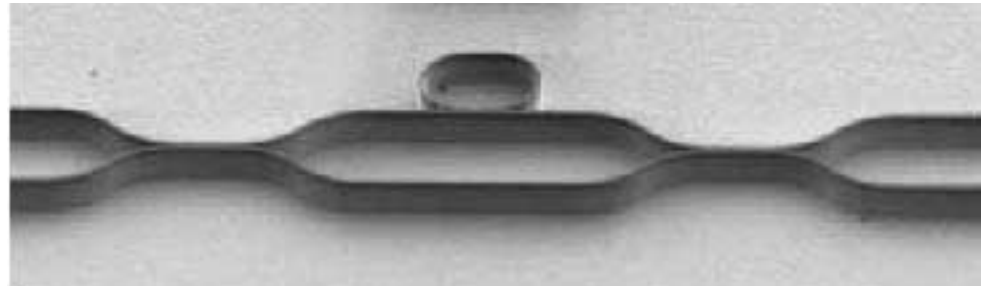
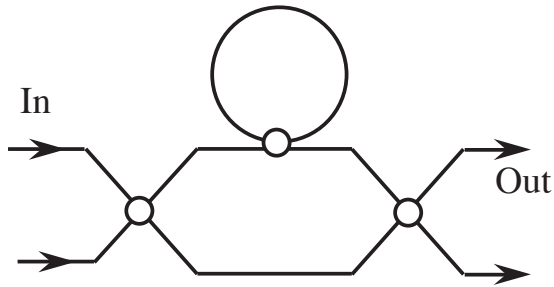
# Laboratory Characterization of Photonic Structures

- Characterization of fiber ring-resonator devices  
(Proof of principle studies)
- Characterization of nanofabricated devices

# Microresonator-Based Add-Drop Filter

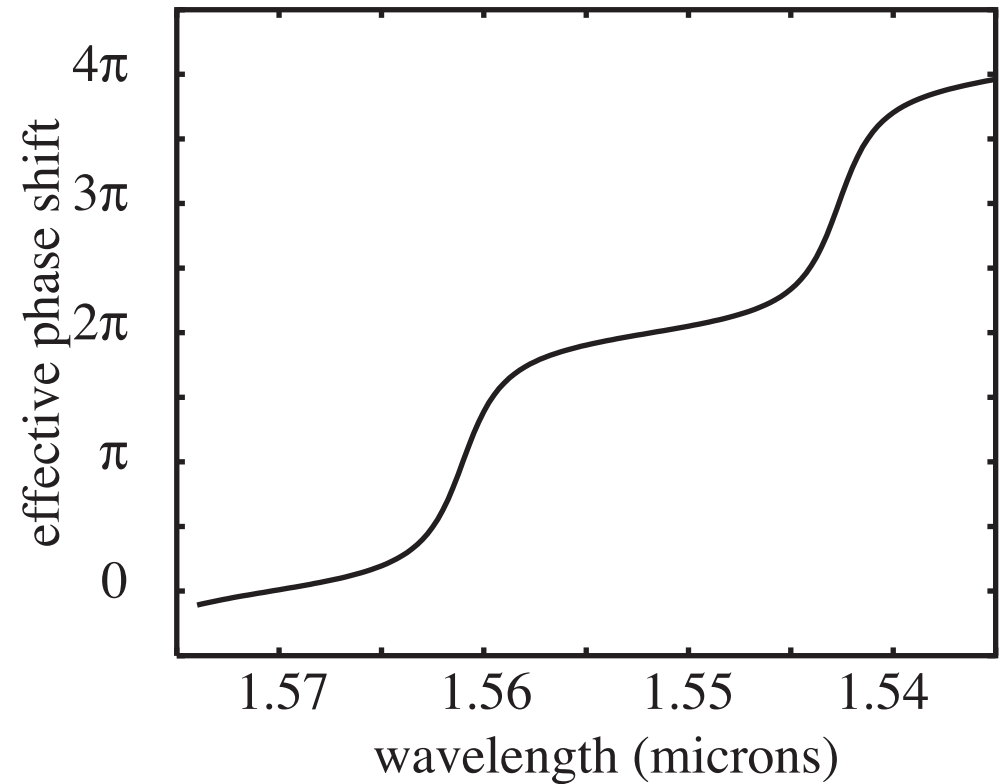
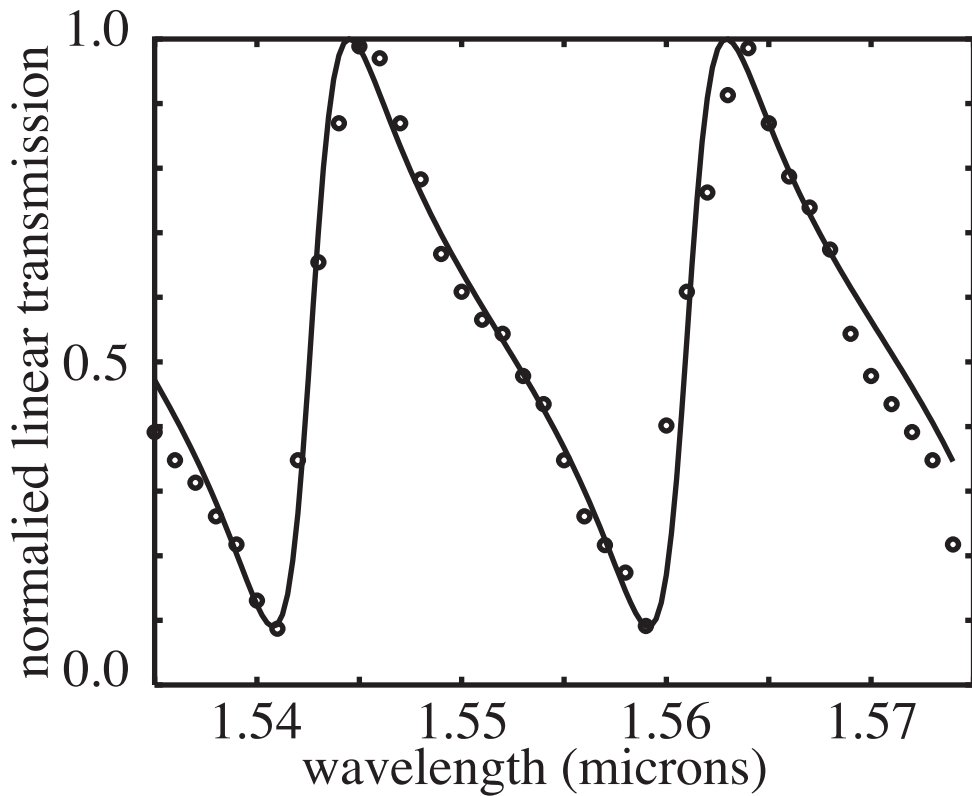


# Phase Characteristics of Micro-Ring Resonator

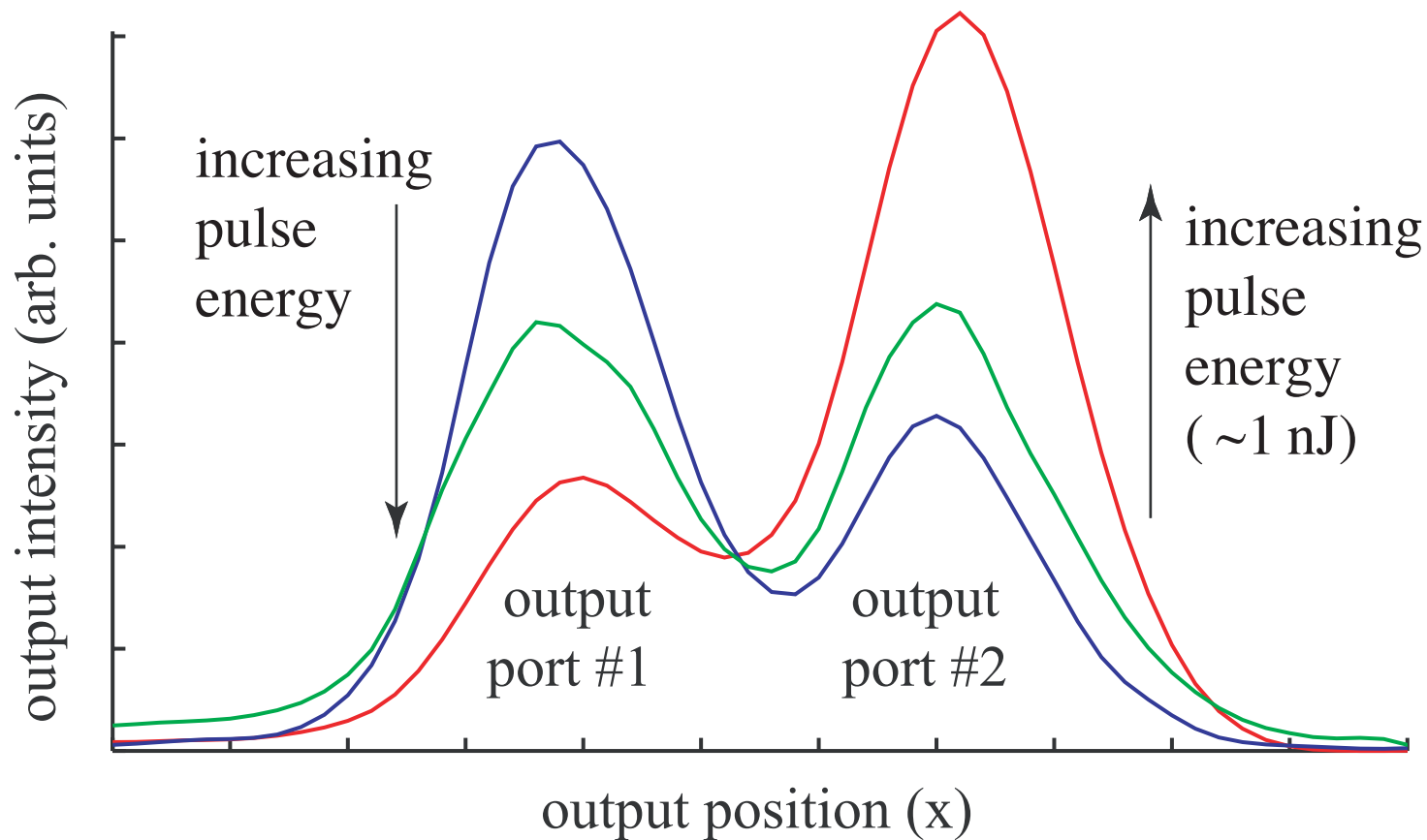
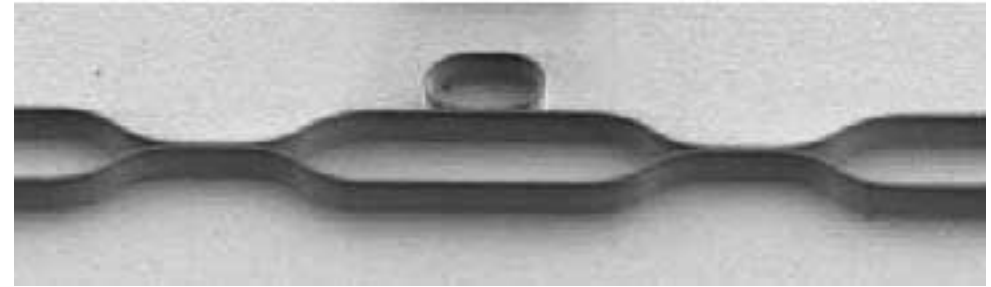
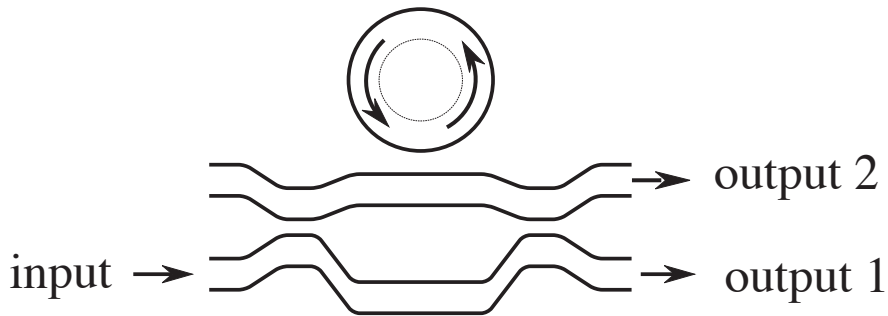


transmission

induced phase shift



# All-Optical Switching in a Microresonator-Enhanced Mach-Zehnder Interferometer



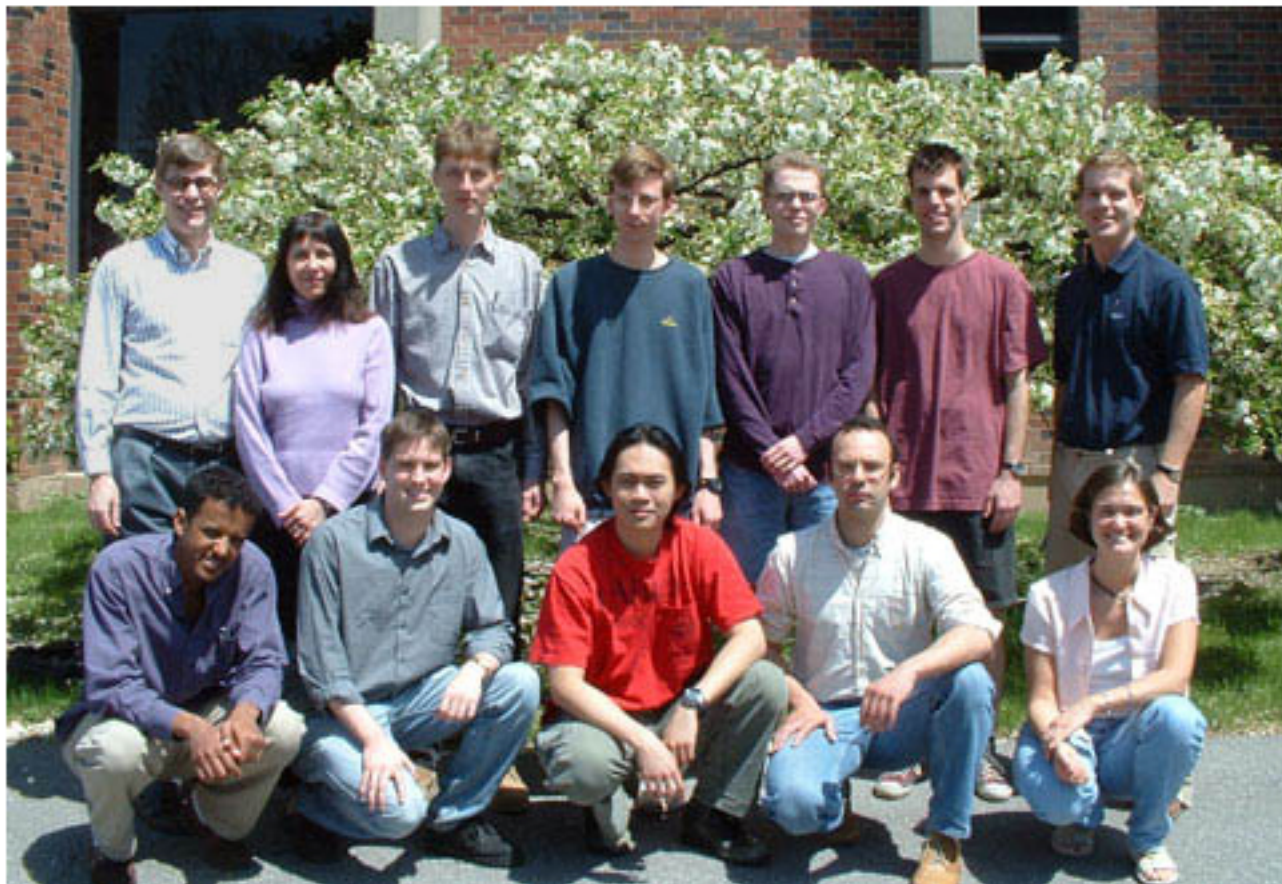
# Summary

Demonstration of slow light propagation in ruby and superluminal light propagation in alexandrite

Argue that artificial materials hold great promise for applications in photonics because of

- large controllable nonlinear response
- large dispersion controllable in magnitude and sign

## Special Thanks to my Students and Research Associates

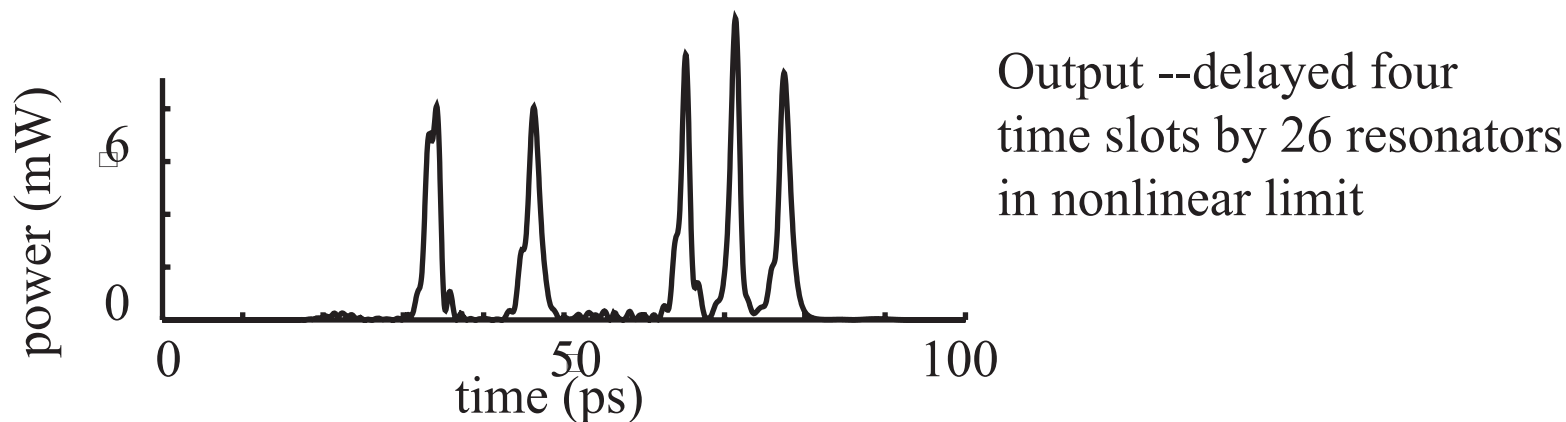
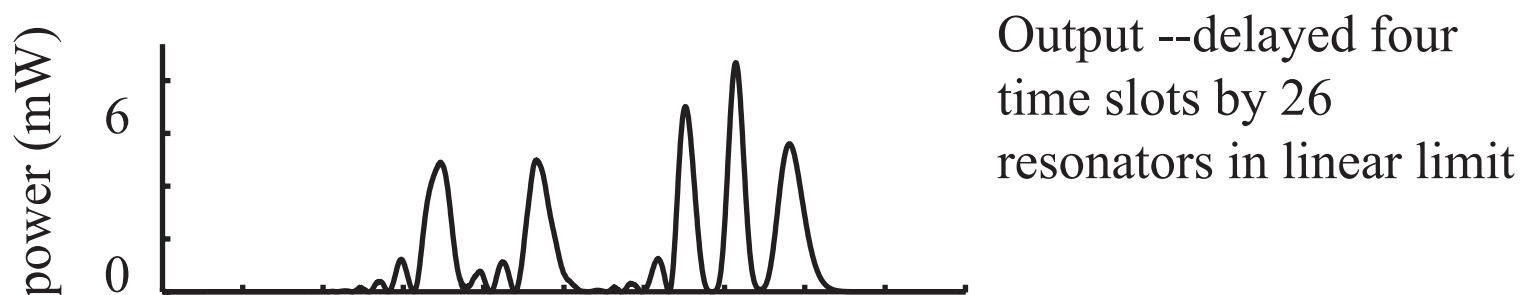
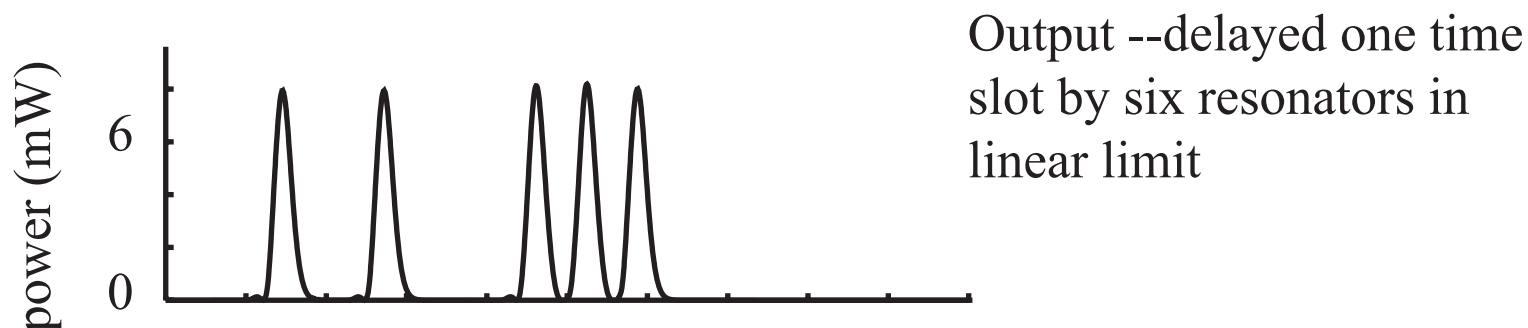
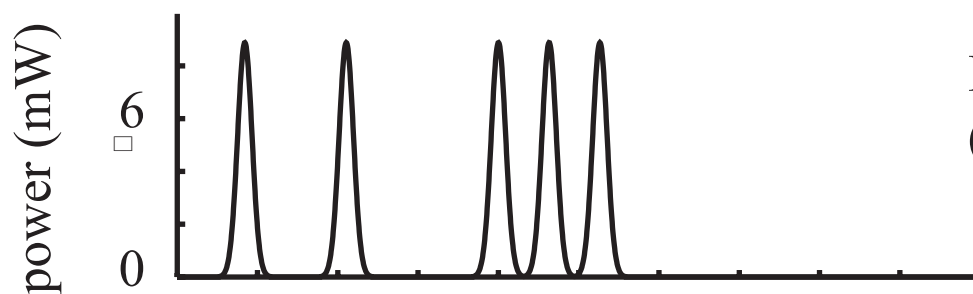


**Thank you for your attention.**

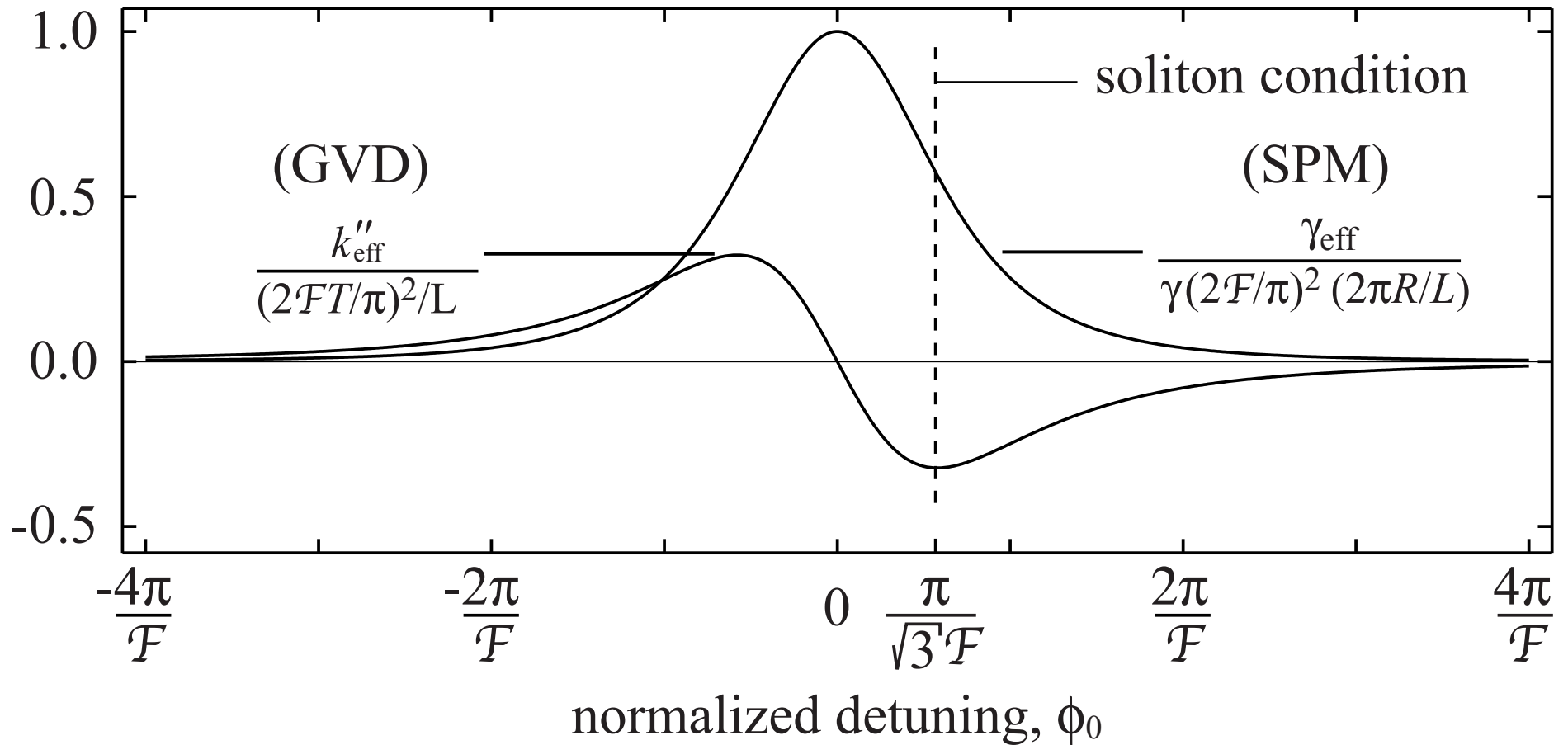


# Photonic Structures -- What Next?

# Performance of SCISSOR as Optical Delay Line



# Frequency Dependence of GVD and SPM Coefficients



# Soliton Propagation

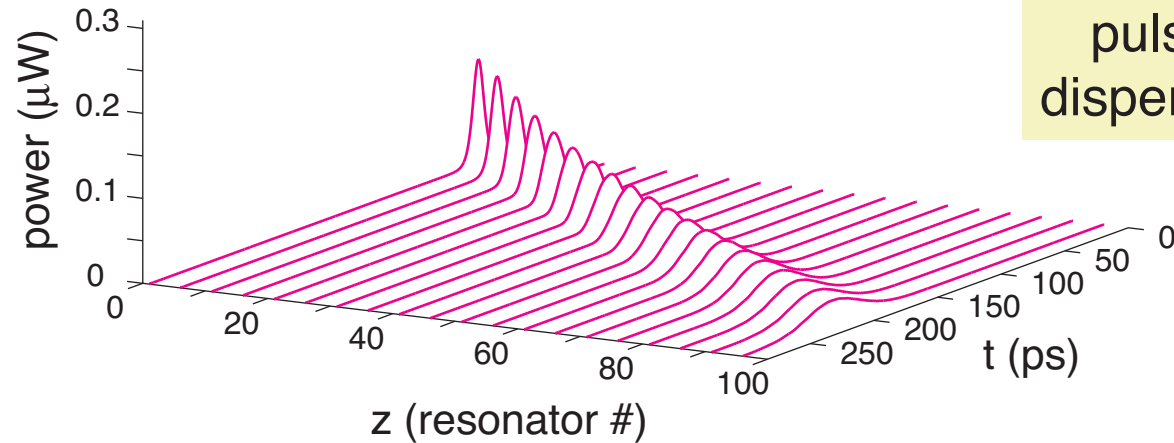
5  $\mu\text{m}$  diameter resonators with a finesse of 30

SCISSOR may be constructed from 100 resonators spaced by 10  $\mu\text{m}$  for a total length of 1 mm

soliton may be excited via a 10 ps, 125mW pulse

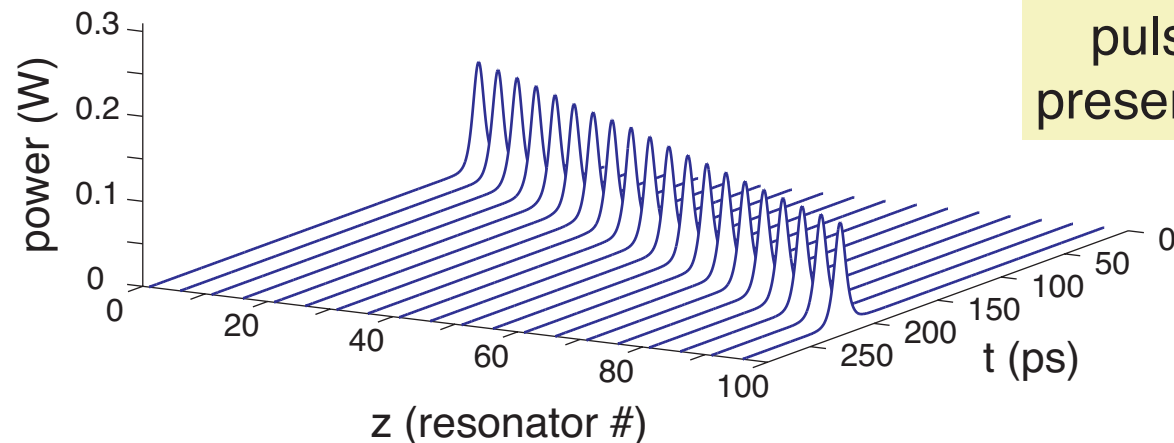
simulation assumes a chalcogenide/GaAs-like nonlinearity

## Weak Pulse



pulse disperses

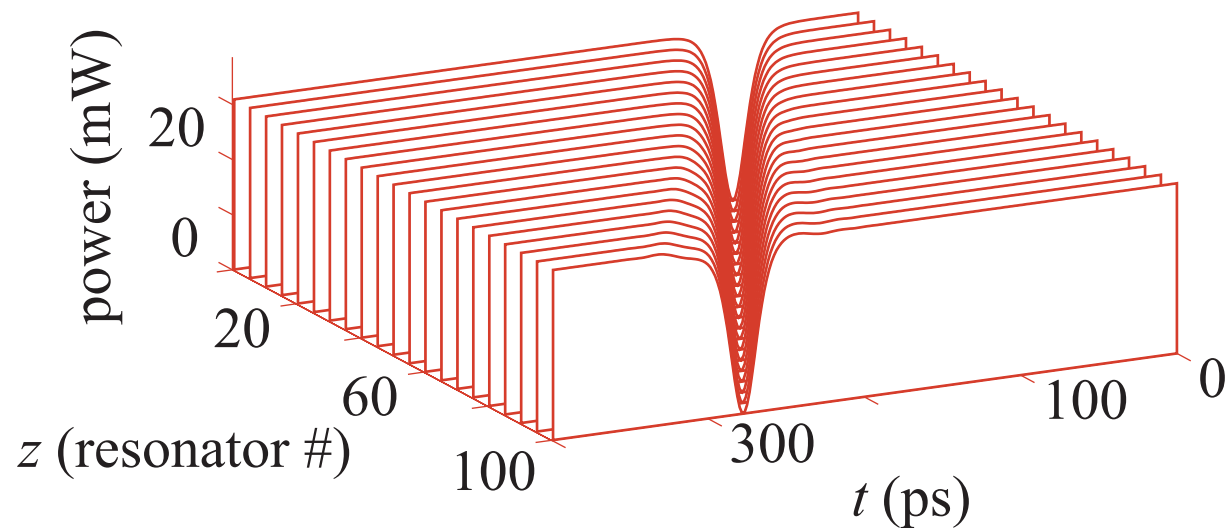
## Fundamental Soliton



pulse preserved

# Dark Solitons

SCISSOR system also supports the propagation of dark solitons.

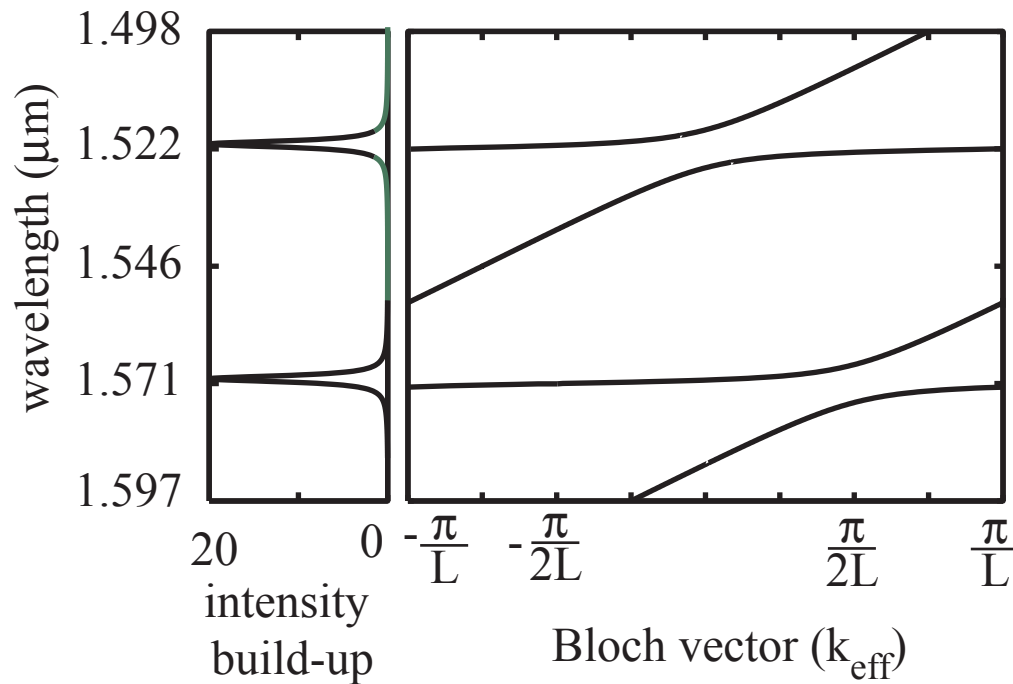


# SCISSOR Dispersion Relations

## Single-Guide SCISSOR

No bandgap

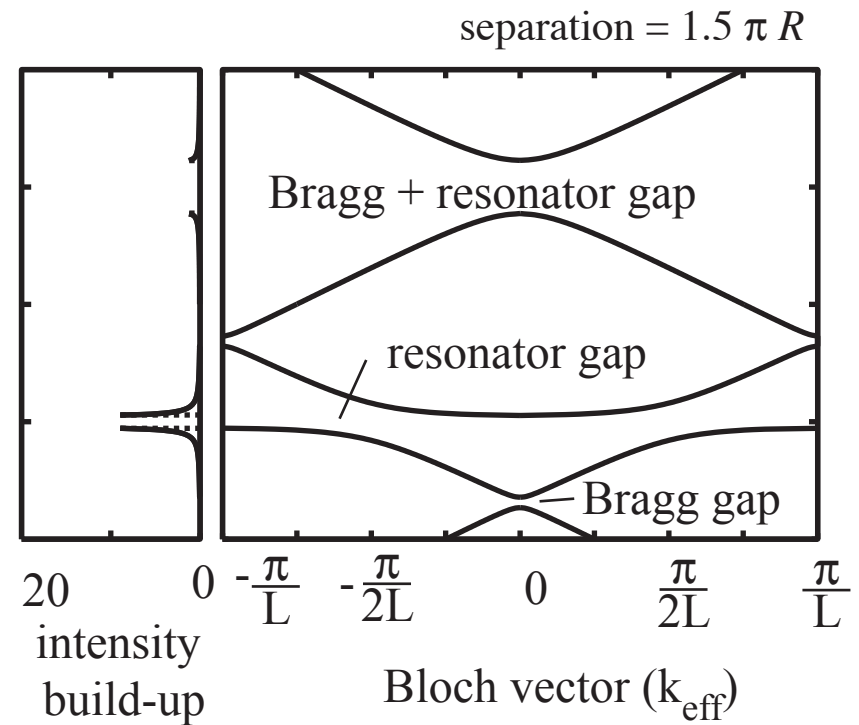
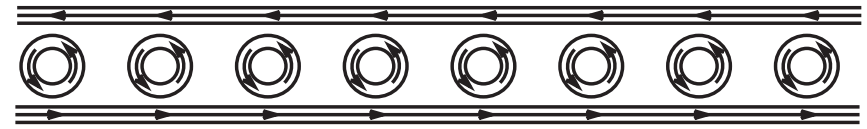
Large intensity buildup



## Double-Guide SCISSOR

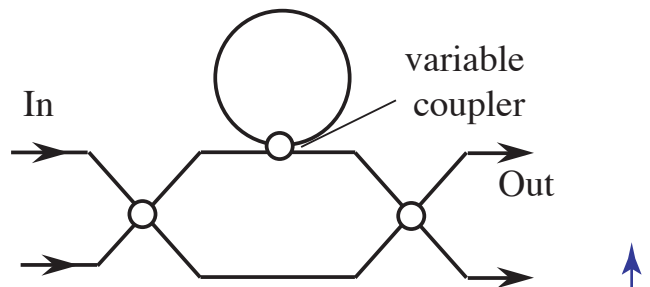
Bandgaps occur

Reduced intensity buildup



# Phase Characteristics of Fiber Ring Resonator

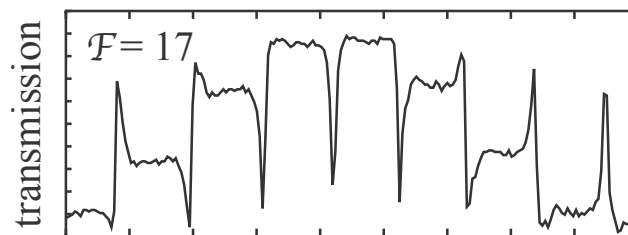
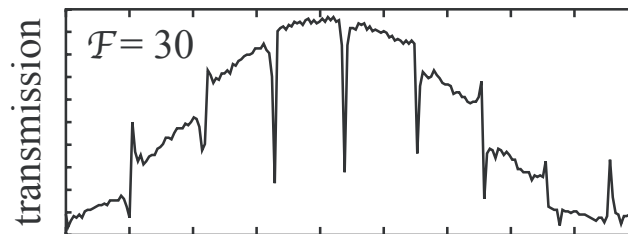
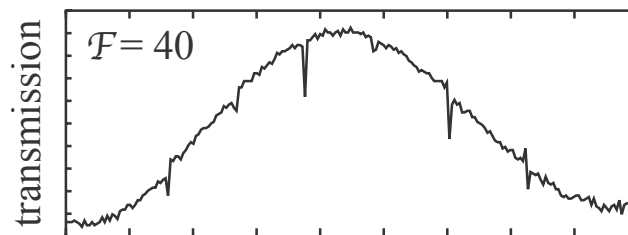
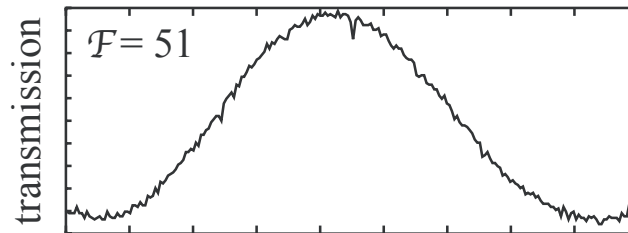
Place ring resonator inside Mach-Zehnder interferometer and measure transmission versus wavelength.



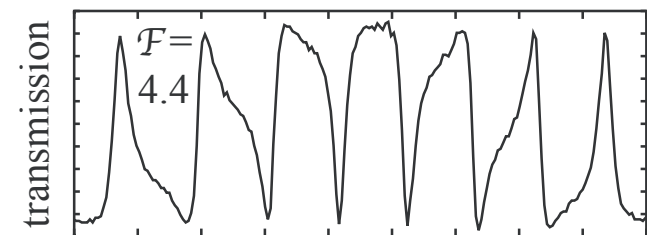
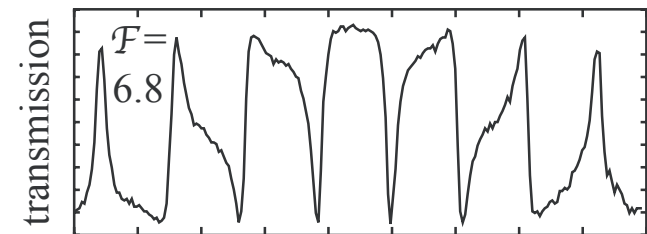
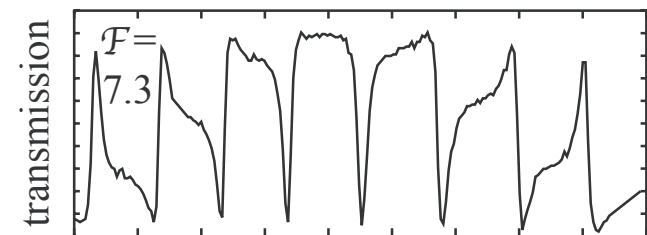
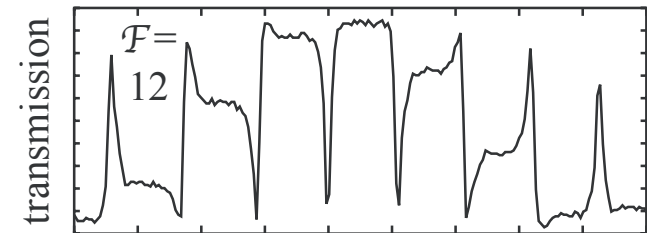
undercoupled

critically coupled

overcoupled



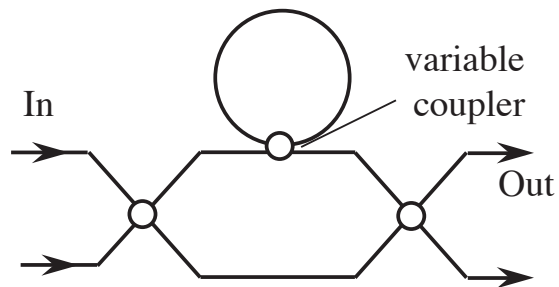
0 10 20 30 40  
 $\Delta$  wavelength (pm)



0 10 20 30 40  
 $\Delta$  wavelength (pm)

# Phase Characteristics of Fiber Ring Resonator

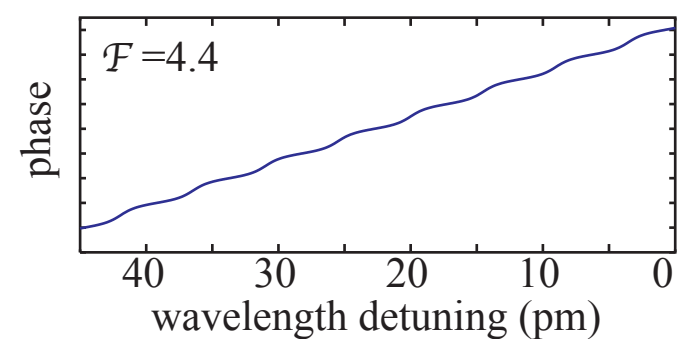
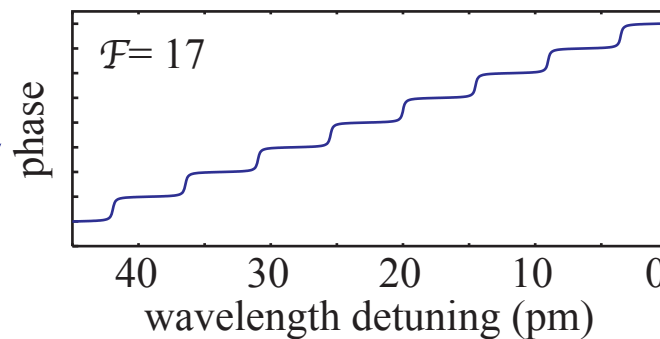
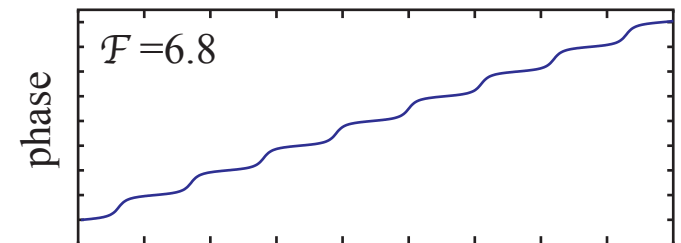
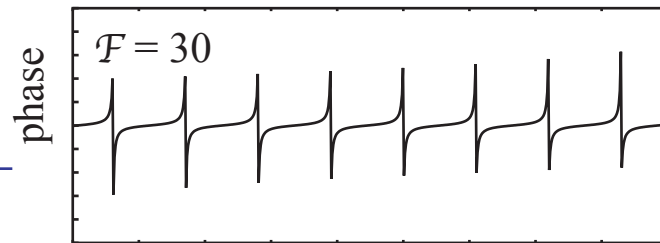
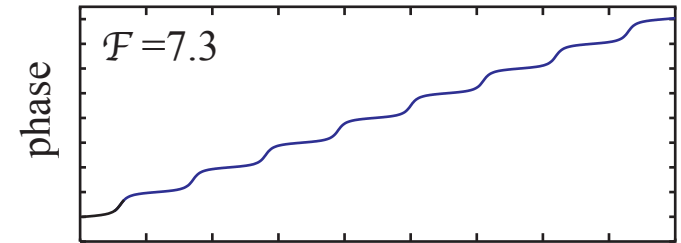
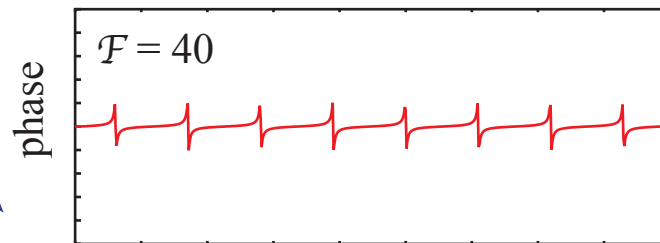
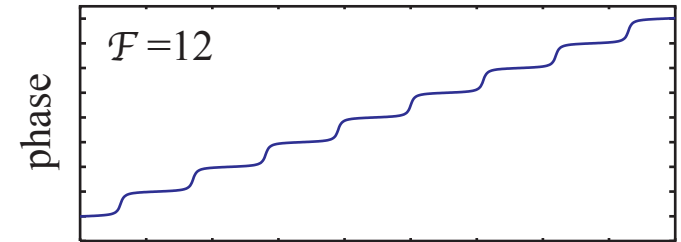
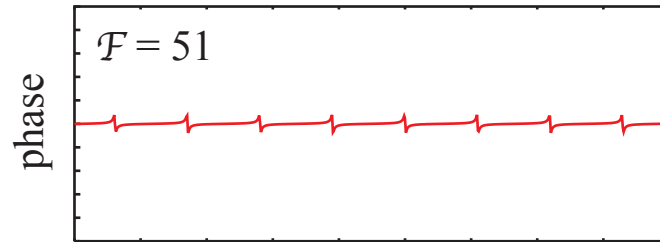
Extracted phase structure



undercoupled

critically coupled

overcoupled





# "Fast" (Superluminal) Light in SCISSOR Structures

Requires **loss** in resonator structure

